

#### Neurocomputing Modern neural networks

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#### Shallow vs. deep networks



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- inputs and outputs.
- may need too many hidden neurons.
- cannot become complex enough.

#### • Universal approximation theorem (Cybenko, 1989): a **shallow** network can approximate any mapping function between

• If the mapping function is too complex, a shallow network

• The hidden neurons extract **features** in the input space: typical characteristics of the input which, when combined by the output neurons, allow to solve the classification task.

• Problem: the features are not hierarchically organized and

#### **Feature selection**



- Shallow networks can not work directly with raw images: noise, translation, rotation, scaling...
- One needs first to extract complex and useful features from the input images in order to classify them correctly.

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# **Deep Neural Network**

- A MLP with more than one hidden layer is a **deep neural network**.
- The different layers extract increasingly complex features.

Deep neural networks learn hierarchical feature representations

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# **Problems with deep networks**

- In practice, training a deep network is not as easy as the theory would suggest.
- Four main problems have to be solved:

- 1. Bad convergence: the loss function has many local minima.
  - Momentum, adaptive optimizers, annealing...
- 2. Long training time: deep networks use gradient descent-like optimizers, an iterative method whose speed depends on initialization.
  - Normalized initialization, batch normalization...
- 3. **Overfitting**: deep networks have a lot of free parameters, so they tend to learn by heart the training set.
  - Regularisation, dropout, data augmentation, early-stopping...
- 4. Vanishing gradient: the first layers may not receive sufficient gradients early in training.
  - ReLU activation function, unsupervised pre-training, residual networks...

# 1 - Bad convergence

# Local minima

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• The loss function  $\mathcal{L}( heta)$  of a deep neural network has usually not a single global minimum, but many local minima: irregular loss landscape.



- Gradient descent gets stuck in local minima by design.
- One could perform different weight initializations, in order to find per chance an initial position close enough from the global minimum.  $\rightarrow$  **inefficient**.

### **Stochastic gradient descent**

• What we actually want to minimize is the mathematical expectation of the square error (or any other loss) on the distribution of the data.

$$\mathcal{L}( heta) = \mathbb{E}_{\mathcal{D}}(||\mathbf{t}-\mathbf{y}||^2)$$

- We do not have access to the true distribution of the data, so we have to estimate it through sampling.
- Batch gradient descent estimates the loss function Online gradient descent estimates the loss by sampling the whole training set:

$$\mathcal{L}( heta) pprox rac{1}{N} \sum_{i=1}^N ||\mathbf{t}_i - \mathbf{y}_i||^2$$

- The estimated gradient is then unbiased (exact) and has no variance.
- Batch GD gets stuck in local minima.

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function by sampling a single example:

$$\mathcal{L}( heta) pprox ||\mathbf{t}_i - \mathbf{y}_i||^2$$

• The estimated gradient has a high variance (never right) but is unbiased on average.

Online GD avoids local minima, but also global minima (unstable)...

#### Stochastic gradient descent

• Stochastic gradient descent samples minibatches of  $K \sim 100$  examples to approximate the mathematical expectation.

$$egin{aligned} \mathcal{L}( heta) &= E_{\mathcal{D}}(||\mathbf{t}-\mathbf{y}||^2) pprox rac{1}{K}\sum_{i=1}^K ||\mathbf{t}_i-\mathbf{y}_i||^2 \ &\Delta heta &= -\eta \, 
abla_ heta \, \mathcal{L}( heta) \end{aligned}$$

- This sampled loss has a high variance: take another minibatch and the gradient of the loss function will likely be very different.
- If the batch size is big enough, the estimated gradient is wrong, but usable on average (unbiased).
- The high variance of the estimated gradient helps getting out of local minimum: because our estimation of the gradient is often **wrong**, we get out of the local minima although we should have stayed in it.
  - The true gradient is 0 for a local minimum, but its sampled value may not, so the parameters will be updated and hopefully get out of the local minimum.
- Which batch size works the best for my data? Cross-validation, but beware that big batch sizes increase memory consumption, what can be a problem on GPUs.



# **Parameter-dependent optimization**

• Another issue with stochastic gradient descent is that it uses the same learning rate for all parameters. In ravines (which are common around minima), some parameters (or directions) have a higher influence on the loss function than others.



Source: https://distill.pub/2017/momentum/

- In the example above, you may want to go faster in the "horizontal" direction than in the "vertical" one, although the gradient is very small in the horizontal direction.
- With a fixed high learning rate for all parameters, SGD would start oscillating for the steep parameters, while being still very slow for the flat ones.
- The high variance of the sampled gradient is detrimental to performance as it can lead to oscillations.
- Most modern optimizers have a parameter-dependent adaptive learning rate.

# SGD with momentum

- One solution is to **smooth** the gradients over time (i.e. between minibatches), in order to avoid that one parameter is increased by one minibatch and decreased by the next one.
- The momentum method uses a **moving average** of the gradient (momentum step) to update the parameters:

$$egin{aligned} v( heta) &= lpha \, v( heta) - (1-lpha) \, 
abla_ heta \, \mathcal{L}( heta) \ &\Delta heta &= \eta \, v( heta) \end{aligned}$$

- $0 \leq \alpha < 1$  controls how much of the gradient we use for the parameter update (usually around 0.9)
- lpha=0 is the vanilla SGD.

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• SGD with momentum uses an **adaptive learning rate**: the learning is implicitly higher when the gradient does not reverse its sign (the estimate "accelerates").

#### SGD with momentum

#### • When the gradient for a single parameter has always the same direction between successive examples, gradient descent accelerates (bigger steps).

- When its sign changes, the weight changes continue in the same direction for while, allowing to "jump" over small local minima if the speed is sufficient.
- If the gradient keeps being in the opposite direction, the weight changes will finally reverse their direction.

# SGD with momentum



- With momentum, the flat parameters keep increasing their update speed, while the steep ones slow down.
- SGD with momentum gets rid of oscillations at higher learning rates.
- The momentum method benefits a lot from the variance of SGD: noisy gradients are used to escape local minima but are averaged around the global minimum.
- See the great visualization by Gabriel Goh on https://distill.pub/2017/momentum/.

used, and creates its own oscillations. What is going on?

# **SGD** with Nesterov momentum

#### Standard Momentum (black) vs Nesterov Momentum (red)



- minimum.

Source: https://ikocabiyik.com/blog/en/visualizing-ml-optimizers/



Source: https://cs231n.github.io/neural-networks-3/

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• SGD with momentum tends to oscillate around the

• The Nesterov momentum **corrects** these oscillations by estimating the gradient after the momentum update:

$$egin{aligned} &=lpha\,v( heta)-(1-lpha)\,
abla_ heta\,\mathcal{L}( heta+lpha\,v( heta))\ &\Delta heta&=\eta\,v( heta) \end{aligned}$$

## **RMSprop**

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- Instead of smoothing the gradient, what destroys information, one could adapt the learning rate to the curvature of the loss function:
  - put the brakes on when the function is steep (high gradient).
  - accelerate when the loss function is flat (plateau).
- RMSprop (Root Mean Square Propagation) scales the learning rate by a running average of the squared gradient (second moment  $\approx$  variance).

$$egin{aligned} v( heta) &= lpha \, v( heta) + (1-lpha) \, (
abla) \ \Delta & heta &= -rac{\eta}{\epsilon + \sqrt{v( heta)}} \, 
abla heta \end{aligned}$$

- If the gradients vary a lot between two minibatches, the learning rate is reduced.
- If the gradients do not vary much, the learning rate is increased.

 $abla_ heta \, \mathcal{L}( heta))^2$  .

 $\mathcal{L}(\theta)$ 

#### Adam

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• Adam (Adaptive Moment Estimation) builds on the idea of RMSprop, but uses also a moving average of the gradient.

$$egin{aligned} m( heta) &= eta_1 m( heta) + (1 - eta_1) \ v( heta) &= eta_2 v( heta) + (1 - eta_2) \, \nabla \ \Delta heta &= -\eta \, rac{m( heta)}{\epsilon + \sqrt{v( heta)}} \end{aligned}$$

- Adam = RMSprop + momentum.
- Other possible optimizers: Adagrad, Adadelta, AdaMax, Nadam...
- In practice, SGD with momentum allows to find better solutions, but the meta-parameters are harder to find (cross-validation).
- Adam finds slightly poorer solutions, but the parameters  $eta_1$ ,  $eta_2$  and  $\epsilon$  can usually be kept at default.

 $egin{aligned} & 
abla_{ heta} \, \mathcal{L}( heta) \ & 
abla_{ heta} \, \mathcal{L}( heta)^2 \end{aligned}$ 

# <del>7</del>)

### **Comparison of modern optimizers**



Source: Alec Radford https://imgur.com/a/Hqolp

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2

0

-2

-4

# **Optimizers in keras https://keras.io/api/optimizers**

• SGD:

```
optimizer = tf.keras.optimizers.SGD(learning_rate=0.01)
```

• SGD with Nesterov momentum:

optimizer = tf.keras.optimizers.SGD(learning\_rate=0.01, momentum=0.9, nesterov=True)

• RMSprop:

```
optimizer = tf.keras.optimizers.RMSprop(
    learning_rate=0.001, rho=0.9, momentum=0.0, epsilon=1e-07
```

• Adam:

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```
optimizer = tf.keras.optimizers.Adam(
    learning_rate=0.001, beta_1=0.9, beta_2=0.999, epsilon=1e-07)
```

# Hyperparameters annealing

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# Finding a good range for the learning rate

- A simple trick to find a good estimate of the learning rate (or its start/stop value) is to increase its value exponentially for each minibatch at the beginning of learning.
- The "good" region for the learning rate is the one where the validation loss decreases, but does not oscillate.



Source: https://towardsdatascience.com/advanced-topics-in-neural-networks-f27fbcc638ae

#### Hyperparameter search



- of the hyperparameters.
- - lognormal).

Source: http://cs231n.github.io/neural-networks-3/

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• Even with annealing, it is tricky to find the optimal value

• The only option is to perform **cross-validation**, by varying the hyperparameters systematically and initializing the weights randomly every time.

• There are two basic methods:

• **Grid search**: different values of each parameter are chosen linearly ( $[0.1, 0.2, \ldots, 0.9]$ ) or logarithmically ( $[10^{-6}, 10^{-5}, \dots, 10^{-1}]$ ).

Random search: the value are randomly chosen each time from some distribution (uniform, normal,

• The advantage of random search is that you can stop it anytime if you can not wait any longer.

• Very time-consuming, but easy to perform in parallel if you have clusters of CPUs or GPUs (data-parallel).

# **Bayesian hyperparameter optimization**

- A more advanced and efficient technique is **Bayesian hyperparameter optimization**, for example the **Tree Parzen Estimator** (TPE) algorithm.
- The idea is to build a probability model of the objective function and use it to select the most promising hyperparameters to evaluate in the true objective function.
- Roughly speaking, it focuses parameter sampling on the interesting regions.
- The hyperopt Python library https://github.com/hyperopt/hyperopt is extremely simple to use:

```
from hyperopt import fmin, tpe, hp, STATUS_OK
def objective(eta):
    # Train model with:
    optimizer = tf.keras.optimizers.SGD(eta)
    return {'loss': test_loss, 'status': STATUS_OK }
best = fmin(objective,
    space=hp.loguniform('eta', -6, -1),
    algo=tpe.suggest,
    max_evals=100)
```

print(best)

• Other library: optuna https://optuna.org



Source: https://towardsdatascience.com/a-conceptualexplanation-of-bayesian-model-based-hyperparameteroptimization-for-machine-learning-b8172278050f

# 2 - Long training times

# Importance of weight initialization



- If the data is not centered in the input space, the hyperplane (i.e. each neuron) may need a lot of iterations to "move" to the correct position using gradient descent. The initialization of the weights will matter a lot: if you start too far away from the solution, you will need many iterations.
- If the data is normalized (zero mean, unit variance), the bias can be initialized to 0 and will converge much faster. Only the **direction** of the weight vector matters, not its norm, so it will be able to classify the data much faster.

### **Data normalization**



Source : http://cs231n.github.io/neural-networks-2/

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- In practice, the input data X must be normalized before training, in order to improve the training time:
  - Mean removal or zero-centering:

$$X' = X - \mathbb{E}(X)$$

• Normalization : mean removal + unit variance:

$$X' = rac{X - \mathbb{E}(X)}{\mathrm{Std}(X)}$$



Source : http://cs231n.github.io/neural-networks-2/

- Whitening goes one step further by first decorrelating the input dimensions (using Principal Component Analysis PCA) and then scaling them so that the data lies in the unit sphere.
- Better method than simple data normalization, but computationally expensive.
- When predicting on new data, do not forget to normalize/whiten them too!

# **Batch normalization (BN)**



- A single layer can learn very fast if its inputs are normalized with zero mean and unit variance.
- This is easy to do for the first layer, as one only need to preprocess the inputs  $\mathbf{x}$ , but not the others.
- The outputs of the first layer are not normalized anymore, so learning in the second layer will be slow.

#### **Batch normalization (BN)**

**Input:** Values of x over a mini-batch:  $\mathcal{B} = \{x_{1...m}\};\$ Parameters to be learned:  $\gamma$ ,  $\beta$ **Output:**  $\{y_i = BN_{\gamma,\beta}(x_i)\}$  $\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^{m} x_i$ // mini-batch mean  $\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2$ // mini-batch variance  $\widehat{x}_i \leftarrow \frac{x_i - \mu \beta}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}}$ // normalize  $y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv BN_{\gamma,\beta}(x_i)$ // scale and shift

Algorithm 1: Batch Normalizing Transform, applied to activation x over a mini-batch.

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lacksquare

- The mean and variance will vary from one minibatch to another, but it does not matter.
- At the end of learning, the mean and variance over the whole training set is computed and stored.
- BN allows to more easily initialize the weights relative to the input strength and to use higher learning rates.

#### **Batch normalization** allows each layer to normalize its inputs on a **single minibatch**:

$$X'_{\mathcal{B}} = rac{X_{\mathcal{B}} - E(X_{\mathcal{B}})}{\operatorname{Std}(X_{\mathcal{B}})}$$

## **Batch normalization (BN)**

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Source : http://heimingx.cn/2016/08/18/cs231n-neural-networks-part-2-setting-up-the-Data-and-the-loss/

- The **Batch Normalization** layer is usually placed between the FC layer and the activation function.  $\bullet$
- It is differentiable w.r.t the input layer and the parameters, so backpropagation still works.

### Weight initialization

- Weight matrices are initialized randomly, but how they are initialized impacts performance a lot.
- There are empirical rules to initialize the weights between two layers with  $N_{
  m in}$  and  $N_{
  m out}$  neurons.
  - **Xavier**: Uniform initialization (when using logistic or tanh, Glorot and Bengio, 2010):

$$W \in \mathcal{U}(-\sqrt{rac{6}{N_{ ext{in}}+N_{ ext{out}}}},\sqrt{rac{6}{N_{ ext{in}}+N_{ ext{out}}}})$$

• He: Gaussian initialization (when using ReLU or PReLU, He et al. 2015):

$$W \in \mathcal{N}(0,\sqrt{rac{2}{N_{ ext{in}}}})$$

- When using BN, the bias b can be initialized to 0.
- Most frameworks (tensorflow, pytorch) initialize the weights correctly for you, but you can also control it.

#### References

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Glorot and Bengio (2010). Understanding the difficulty of training deep feedforward neural networks. AISTATS. He et al. (2015). Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification. arXiv:1502.01852

# 3 - Overfitting



Source : https://www.teco.edu/~albrecht/neuro/html/node10.html

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• The main problem with deep NN is **overfitting**.

With increasing depth, the network has too many weights = free parameters, so its VC dimension is

$$\epsilon = rac{\mathrm{VC_{dim}}}{N}$$

• The network learns the data, not the underlying

- We need to put constraints on the weights to reduce the VC dimension.
  - If the weights move freely (i.e. can take any value), the VC dimension is equal to the number of free parameters.
  - If the weights cannot take any value they like, this implicitly reduces the VC dimension.
- In linear classification, the weights were unconstrained: the norm of the weight vector can take any value, as only its direction is important.



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- Intuition: The norm of the weight vector influences the speed of learning in linear classification.
- A weight update on a strong weight has less influence than on a weak weight:

 $W \leftarrow W + \Delta W = W - \eta \, rac{\partial l( heta)}{\partial W}$ 

as the gradient  $\frac{\partial l(\theta)}{\partial W}$  does not depend on the norm of the weights, only the output error.



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#### **L2 Regularization**

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• L2 regularization keeps the  $\mathcal{L}_2$  norm of the free parameters  $||\theta||$  as small as possible during learning.

$$|| heta||^2 = w_1^2 + w_2^2 + \cdots$$

- Each neuron will use all its inputs with small weights, instead on specializing on a small part with high weights.
- Two things have to be minimized at the same time: the training loss and a **penalty term** representing the norm of the weights:

$$\mathcal{L}( heta) = \mathbb{E}_{\mathcal{D}}(||\mathbf{t}-\mathbf{y}||^2) +$$

- The **regularization parameter**  $\lambda$  controls the strength of regularization:
  - if  $\lambda$  is small, there is only a small regularization, the weights can increase.
  - if  $\lambda$  is high, the weights will be kept very small, but they may not minimize the training loss.

$$+ w_M^2$$

 $\lambda || heta||^2$ 

#### **L2 Regularization**

• MSE loss with L2 regularization penalty term:

$$\mathcal{L}( heta) = \mathbb{E}_{\mathcal{D}}[||\mathbf{t} - \mathbf{y}||^2] +$$

• The gradient of the new loss function is easy to find:

$$abla_ heta \mathcal{L}( heta) = -2\,(\mathbf{t}-\mathbf{y})
abla_ heta\mathbf{y}$$

• Weight updates become:

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$$\Delta heta = \eta \, ({f t} - {f y}) 
abla_{ heta} {f y} \, -$$

- L2 regularization leads to weight decay: even if there is no output error, the weight will converge to 0.
- This forces the weight to constantly learn: it can not specialize on a particular example anymore (overfitting) and is forced to generalize.

#### $\lambda \, || heta||^2$

 $\mathbf{y}+2\,\lambda\, heta$ 

#### $\eta\,\lambda\, heta$

put error, the weight will converge to 0. e on a particular example anymore

# L1 Regularization

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• L1 regularization penalizes the absolute value of the weights instead of their Euclidian norm:

$$\mathcal{L}( heta) = \mathbb{E}_{\mathcal{D}}[||\mathbf{t} - \mathbf{y}||^2] +$$

• It leads to very sparse representations: a lot of neurons will be inactive, and only a few will represent the input.



 $+ \lambda \left| heta 
ight|$ 

#### Dropout

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(a) Standard Neural Net

- Randomly dropping (inactivating) some neurons with a **probability** p between two input presentations reduces the number of free parameters available for each learning phase.
- Multiple smaller networks (smaller VC dimension) are in fact learned in parallel on different data, but they share some parameters.
- This method forces the network to generalize. It is a form of regularization (mathematically equivalent to L2), now preferred in deep networks. p is usually around 0.5.

(b) After applying dropout

#### Dropout

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- Each new input  $\mathbf{x}$  (or minibatch of inputs) is learned by a different neural network.
- But on average, the big neural network has learned the whole dataset without overfitting.



Source: https://towardsdatascience.com/preventing-deep-neural-network-from-overfitting-953458db800a

### **Data augmentation**



Source : https://blog.keras.io/building-powerful-image-classification-models-using-very-little-data.html

- The best way to avoid overfitting is to use more data (with variability), but this is not always possible. • A simple trick to have more data is **data augmentation**, i.e. modifying the inputs while keeping the output
- constant.
- For object recognition, it consists of applying various affine transformations (translation, rotation, scaling) on each input image, while keeping the label constant.
- Allows virtually infinite training sets.





- Early-stopping fights overfitting by monitoring the model's performance on a validation set.
- A validation set is a set of examples that we never use for gradient descent, but which is also not a part of the test set.
- If the model's performance ceases to improve sufficiently on the validation set, or even degrades with further optimization, we can either stop learning or modify some meta-parameters (learning rate, momentum, regularization...).
- The validation loss is usually lower than the training loss at the beginning of learning (underfitting), but becomes higher when the network overfits.

# 4 - Vanishing gradient

- Contrary to what we could think, adding more layers to a DNN does not necessarily lead to a better performance, both on the training and test set.
- Here is the performance of neural networks with 20 or 56 layers on CIFAR-10:



• The main reason behind this is the **vanishing gradient problem**.













• The gradient of the loss function is repeatedly multiplied by a weight matrix W as it travels backwards in a deep network.

$$rac{\partial \mathbf{h}_k}{\partial \mathbf{h}_{k-1}} = f'(W^k \, \mathbf{h}_{k-1} + \mathbf{b}^k) \, W^k$$

• When it arrives in the first FC layer, the contribution of the weight matrices is comprised between:

$$(W_{\min})^d$$
 and  $(W_{\max})^d$ 

where  $W_{
m max}$  (resp.  $W_{
m min}$ ) is the weight matrix with the highest (resp. lowest) norm, and d is the depth of the network.

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Source: https://smartstuartkim.wordpress.com/2019/02/09/vanishing-gradient-problem/

- If  $|W_{\max}| < 1$ , then  $(W_{\max})^d$  is very small for high values of d : the gradient vanishes.
- If  $|W_{\min}| > 1$ , then  $(W_{\min})^d$  is very high for high values of d: the gradient explodes.
- Exploding gradients can be solved by gradient clipping, i.e. normalizing the backpropagated gradient if its norm exceeds a threshold (only its direction actually matters).

$$||rac{\partial \mathcal{L}( heta)}{\partial W^k}|| \leftarrow \min(||rac{\partial \mathcal{L}( heta)}{\partial W^k}||,K)$$

- Vanishing gradients are still the current limitation of deep networks.
- Solutions: ReLU, batch normalization + weight initialization, unsupervised pre-training, residual networks...

# **Derivative of the activation function**

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- Old-school MLP used logistic or tanh transfer functions for the hidden neurons, but their gradient is zero for very high or low net activations.
- If a neuron is saturated, it won't transmit the gradient backwards, so the vanishing gradient is even worse.



#### **Choice of the activation function**



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• Deep networks now typically use the ReLU or PReLU activation functions to improve convergence.

$$f'(x) = egin{cases} 1 & ext{if } x > \ lpha & ext{if } x > \ \ext{if } x > \ex$$

• PReLU always backpropagates the gradient, so it helps fighting against vanishing gradient.



 $> 0 \ \leq 0$ 

# **5 - Deep neural networks in practice**

#### **Deep NN in keras**

```
from tf.keras.models import Sequential
from tf.keras.layers import Input, Dense, Dropout, Activation, BatchNormalization
from tf.keras.optimizers import Adam
model = Sequential()
model.add(Input(784,))
model_add(Dense(200))
model.add(BatchNormalization())
model.add(Activation('relu'))
model.add(Dropout(0.5))
model.add(Dense(100)
model.add(BatchNormalization())
model.add(Activation('relu'))
model.add(Dropout(0.5))
model.add(Dense(units=10, activation='softmax'))
```

model.compile(loss='categorical\_crossentropy', optimizer=Adam(lr=0.01, decay=1e-6))

### Take-home messages

If you want to successfully train a deep neural network, you should:

- Use as much data as possible, with **data augmentation** if needed.
- Normalize the inputs.

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- Use batch normalization in every layer and at least ReLU.
- Use a good **optimizer** (SGD with momentum, Adam).
- **Regularize** learning (L2, L1, dropout).
- Track overfitting on the validation set and use early-stopping.
- Search for the best **hyperparameters** using grid search or hyperopt:
  - Learning rate, schedule, momentum, dropout level, number of layers/neurons, transfer functions, etc.



Source: https://xkcd.com/1838/