



UNIVERSITY OF TECHNOLOGY
IN THE EUROPEAN CAPITAL OF CULTURE
CHEMNITZ

Neurocomputing

Recurrent neural networks

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1 - RNN

Problem with feedforward networks

- **Feedforward neural networks** learn to associate an input vector to an output.

$$\mathbf{y} = F_{\theta}(\mathbf{x})$$

- If you present a sequence of inputs $\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_t$ to a feedforward network, the outputs will be independent from each other:

$$\mathbf{y}_0 = F_{\theta}(\mathbf{x}_0)$$

$$\mathbf{y}_1 = F_{\theta}(\mathbf{x}_1)$$

...

$$\mathbf{y}_t = F_{\theta}(\mathbf{x}_t)$$

- Many problems depend on time series, such as predicting the future of a time series by knowing its past values.

$$x_{t+1} = F_{\theta}(x_0, x_1, \dots, x_t)$$

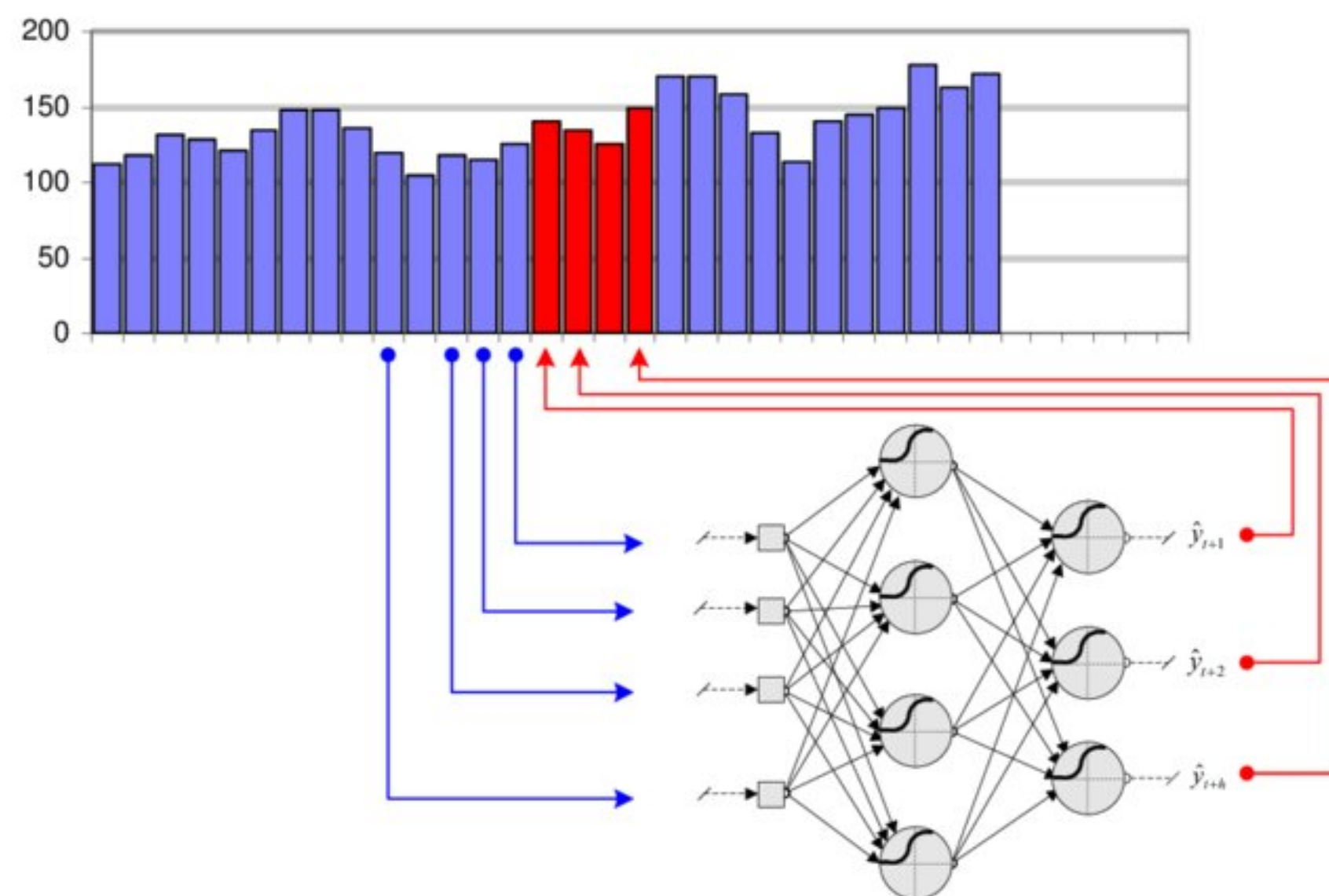
- Example: weather forecast, financial prediction, predictive maintenance, video analysis...

Input aggregation

- A naive solution is to **aggregate** (concatenate) inputs over a sufficiently long window and use it as a new input vector for the feedforward network.

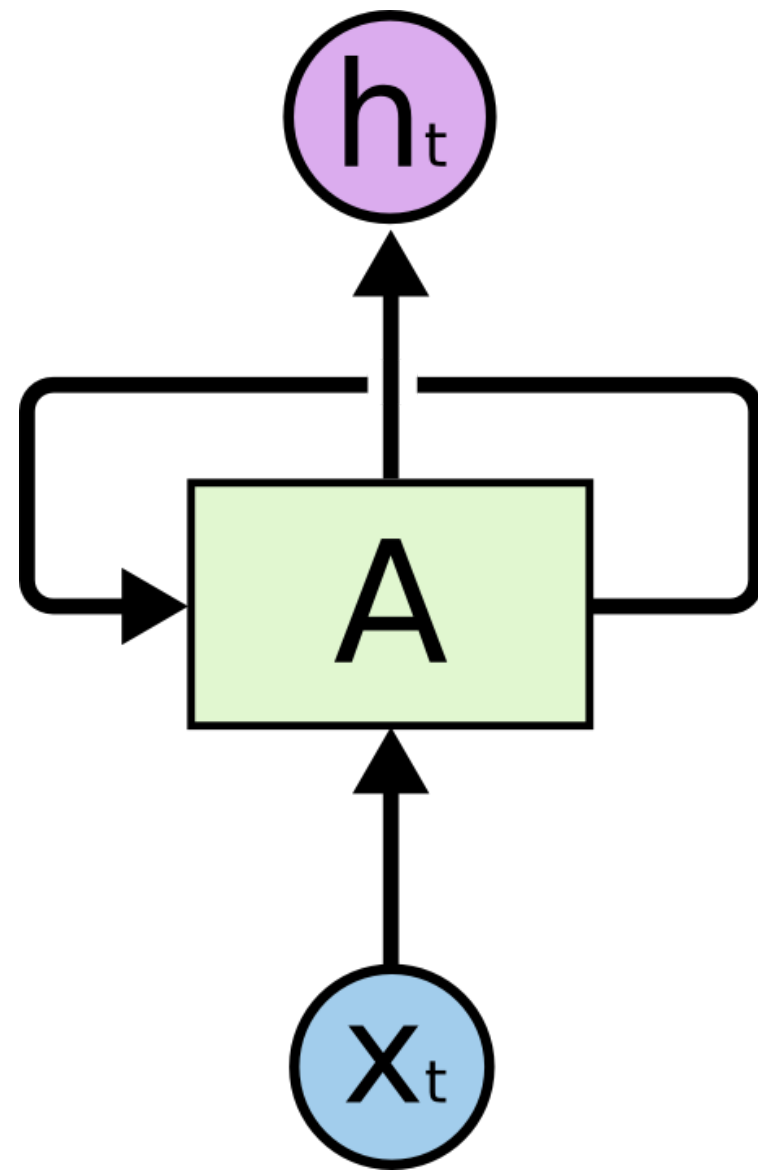
$$\mathbf{X} = [\mathbf{x}_{t-T} \quad \mathbf{x}_{t-T+1} \quad \dots \quad \mathbf{x}_t]$$

$$\mathbf{y}_t = F_{\theta}(\mathbf{X})$$



- **Problem 1:** How long should the window be?
- **Problem 2:** Having more input dimensions increases dramatically the complexity of the classifier (VC dimension), hence the number of training examples required to avoid overfitting.

Recurrent neural network



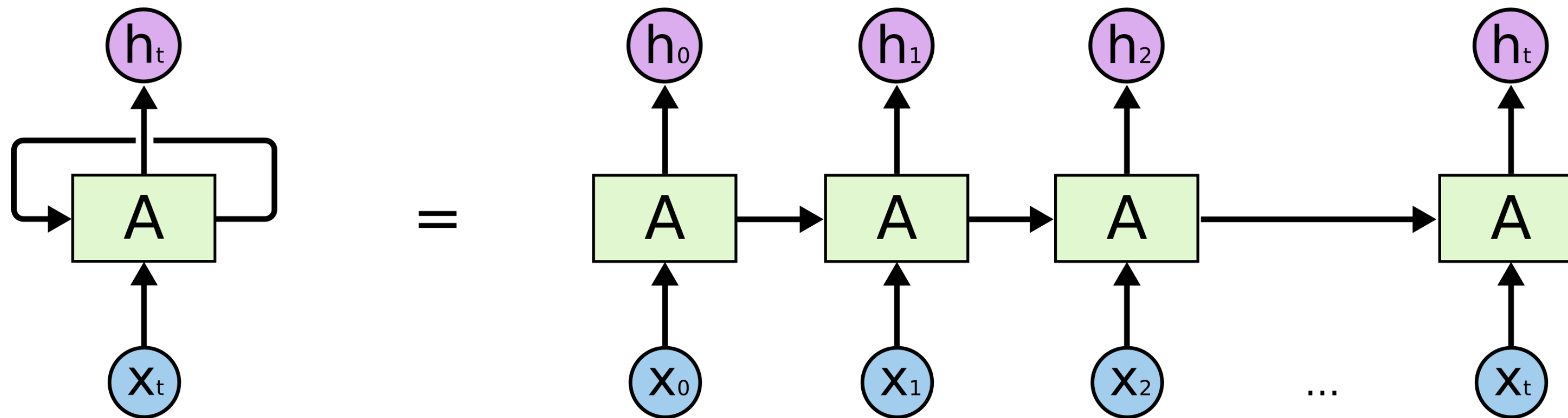
Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

- A **recurrent neural network** (RNN) uses its previous output as an additional input (*context*).
- All vectors have a time index t denoting the time at which this vector was computed.
- The input vector at time t is \mathbf{x}_t , the output vector is \mathbf{h}_t :

$$\mathbf{h}_t = \sigma(W_x \times \mathbf{x}_t + W_h \times \mathbf{h}_{t-1} + \mathbf{b})$$

- σ is a transfer function, usually logistic or tanh.
- The input \mathbf{x}_t and previous output \mathbf{h}_{t-1} are multiplied by **learnable weights**:
 - W_x is the input weight matrix.
 - W_h is the recurrent weight matrix.

Recurrent neural networks



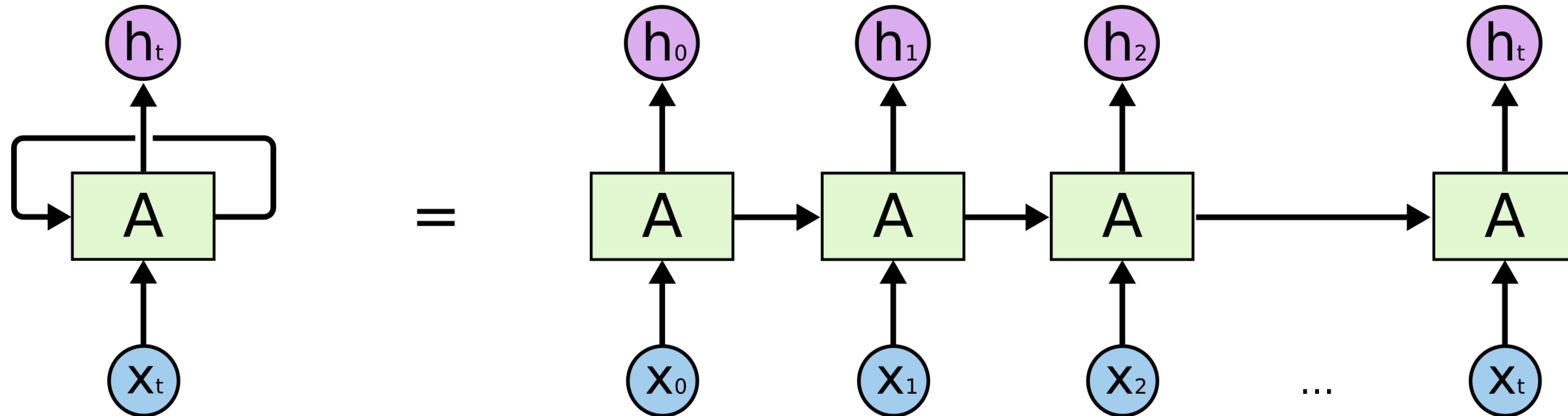
Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

- One can **unroll** a recurrent network: the output \mathbf{h}_t depends on the whole history of inputs from \mathbf{x}_0 to \mathbf{x}_t .

$$\begin{aligned}\mathbf{h}_t &= \sigma(W_x \times \mathbf{x}_t + W_h \times \mathbf{h}_{t-1} + \mathbf{b}) \\ &= \sigma(W_x \times \mathbf{x}_t + W_h \times \sigma(W_x \times \mathbf{x}_{t-1} + W_h \times \mathbf{h}_{t-2} + \mathbf{b}) + \mathbf{b}) \\ &= f_{W_x, W_h, \mathbf{b}}(\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_t)\end{aligned}$$

- A RNN is considered as part of **deep learning**, as there are many layers of weights between the first input \mathbf{x}_0 and the output \mathbf{h}_t .
- The only difference with a DNN is that the weights W_x and W_h are **reused** at each time step.

BPTT: Backpropagation through time



Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

$$\mathbf{h}_t = f_{W_x, W_h, \mathbf{b}}(\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_t)$$

- The function between the history of inputs and the output at time t is differentiable: we can simply apply gradient descent to find the weights!
- This variant of backpropagation is called **Backpropagation Through Time** (BPTT).
- Once the loss between \mathbf{h}_t and its desired value is computed, one applies the **chain rule** to find out how to modify the weights W_x and W_h using the history $(\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_t)$.

BPTT: Backpropagation through time

- Let's compute the gradient accumulated between \mathbf{h}_{t-1} and \mathbf{h}_t :

$$\mathbf{h}_t = \sigma(W_x \times \mathbf{x}_t + W_h \times \mathbf{h}_{t-1} + \mathbf{b})$$

- As for feedforward networks, the gradient of the loss function is decomposed into two parts:

$$\frac{\partial \mathcal{L}(W_x, W_h)}{\partial W_x} = \frac{\partial \mathcal{L}(W_x, W_h)}{\partial \mathbf{h}_t} \times \frac{\partial \mathbf{h}_t}{\partial W_x}$$

$$\frac{\partial \mathcal{L}(W_x, W_h)}{\partial W_h} = \frac{\partial \mathcal{L}(W_x, W_h)}{\partial \mathbf{h}_t} \times \frac{\partial \mathbf{h}_t}{\partial W_h}$$

- The first part only depends on the loss function (mse, cross-entropy):

$$\frac{\partial \mathcal{L}(W_x, W_h)}{\partial \mathbf{h}_t} = -(\mathbf{t}_t - \mathbf{h}_t)$$

- The second part depends on the RNN itself.

BPTT: Backpropagation through time

- Output of the RNN:

$$\mathbf{h}_t = \sigma(W_x \times \mathbf{x}_t + W_h \times \mathbf{h}_{t-1} + \mathbf{b})$$

- The gradients w.r.t the two weight matrices are given by this **recursive** relationship (product rule):

$$\frac{\partial \mathbf{h}_t}{\partial W_x} = \mathbf{h}'_t \times (\mathbf{x}_t + W_h \times \frac{\partial \mathbf{h}_{t-1}}{\partial W_x})$$

$$\frac{\partial \mathbf{h}_t}{\partial W_h} = \mathbf{h}'_t \times (\mathbf{h}_{t-1} + W_h \times \frac{\partial \mathbf{h}_{t-1}}{\partial W_h})$$

- The derivative of the transfer function is noted \mathbf{h}'_t :

$$\mathbf{h}'_t = \begin{cases} \mathbf{h}_t (1 - \mathbf{h}_t) & \text{for logistic} \\ (1 - \mathbf{h}_t^2) & \text{for tanh.} \end{cases}$$

BPTT: Backpropagation through time

- If we **unroll** the gradient, we obtain:

$$\frac{\partial \mathbf{h}_t}{\partial W_x} = \mathbf{h}'_t (\mathbf{x}_t + W_h \times \mathbf{h}'_{t-1} (\mathbf{x}_{t-1} + W_h \times \mathbf{h}'_{t-2} (\mathbf{x}_{t-2} + W_h \times \dots (\mathbf{x}_0))))$$

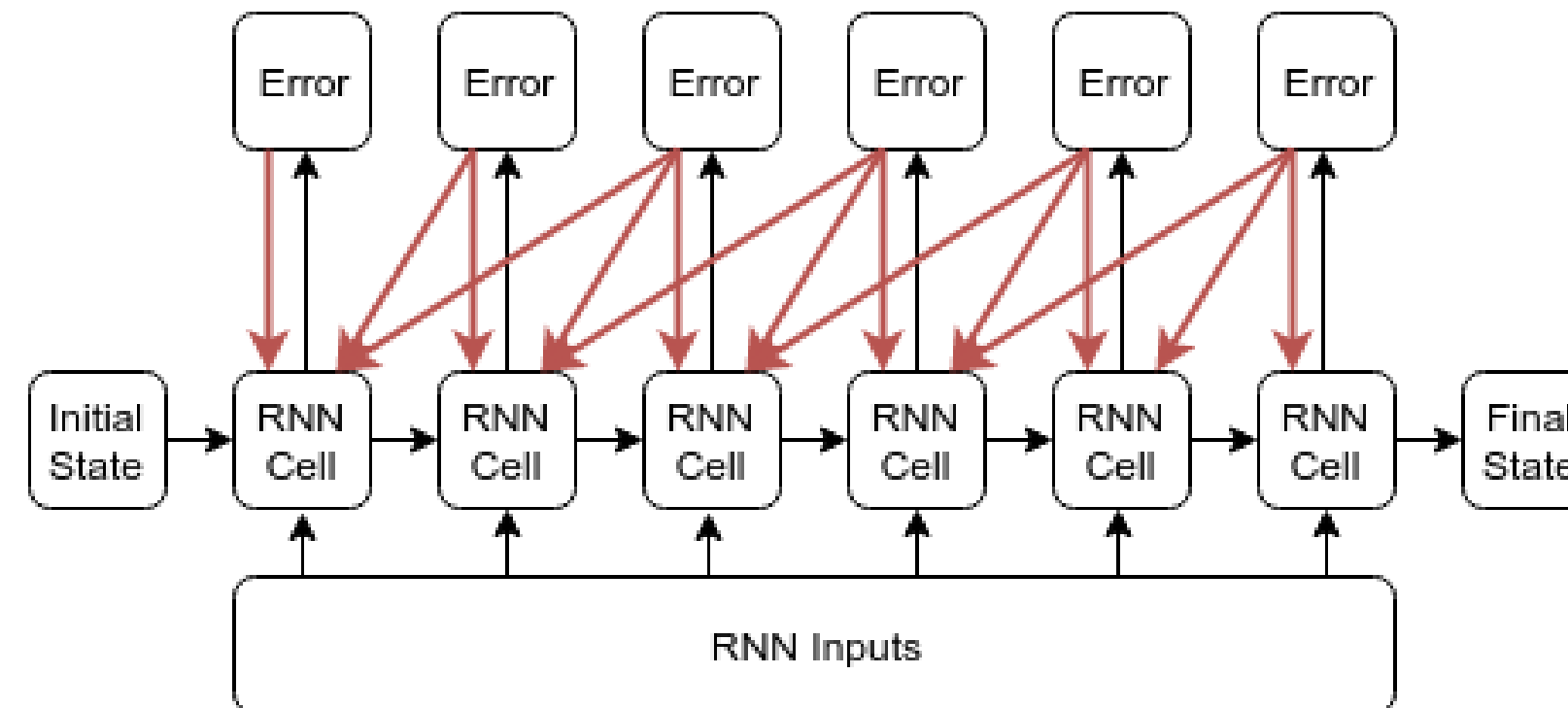
$$\frac{\partial \mathbf{h}_t}{\partial W_h} = \mathbf{h}'_t (\mathbf{h}_{t-1} + W_h \times \mathbf{h}'_{t-1} (\mathbf{h}_{t-2} + W_h \times \mathbf{h}'_{t-2} \dots (\mathbf{h}_0)))$$

- When updating the weights at time t , we need to store in memory:
 - the complete history of inputs $\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_t$.
 - the complete history of outputs $\mathbf{h}_0, \mathbf{h}_1, \dots, \mathbf{h}_t$.
 - the complete history of derivatives $\mathbf{h}'_0, \mathbf{h}'_1, \dots, \mathbf{h}'_t$.

before computing the gradients iteratively, starting from time t and accumulating gradients **backwards** in time until $t = 0$.

- Each step backwards in time adds a bit to the gradient used to update the weights.

Truncated BPTT

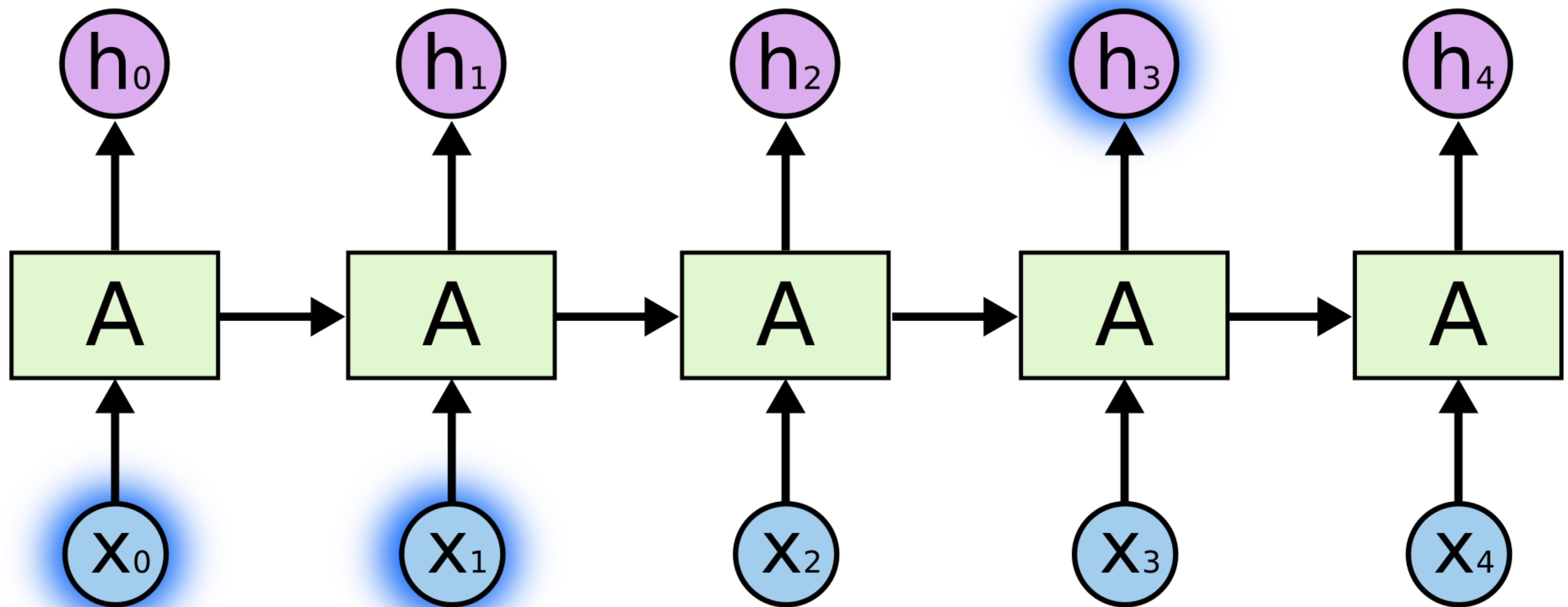


Source: <https://r2rt.com/styles-of-truncated-backpropagation.html>

- In practice, going back to $t = 0$ at each time step requires too many computations, which may not be needed.
- **Truncated BPTT** only updates the gradients up to T steps before: the gradients are computed backwards from t to $t - T$. The partial derivative in $t - T - 1$ is considered 0.
- This limits the **horizon** of BPTT: dependencies longer than T will not be learned, so it has to be chosen carefully for the task.
- T becomes yet another hyperparameter of your algorithm...

Temporal dependencies

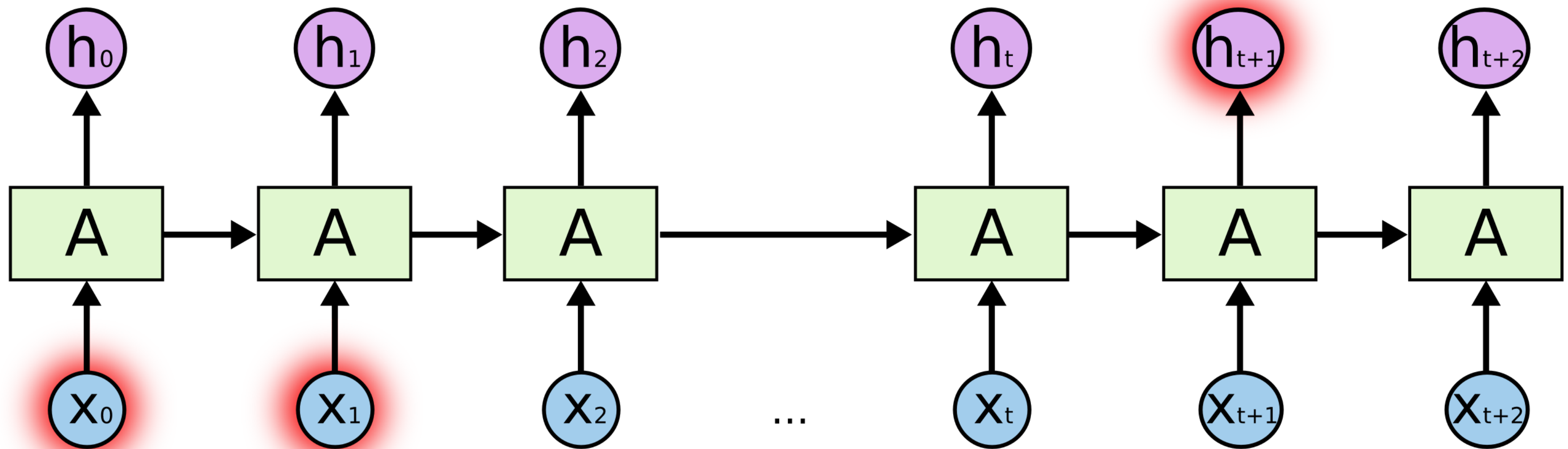
- BPTT is able to find **short-term dependencies** between inputs and outputs: perceiving the inputs \mathbf{x}_0 and \mathbf{x}_1 allows to respond correctly at $t = 3$.



Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

Temporal dependencies

- But it fails to detect **long-term dependencies** because of:
 - the truncated horizon T (for computational reasons).
 - the **vanishing gradient problem**.



Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

Vanishing and exploding gradients

- Let's look at the gradient w.r.t to the input weights:

$$\frac{\partial \mathbf{h}_t}{\partial W_x} = \mathbf{h}'_t (\mathbf{x}_t + W_h \times \frac{\partial \mathbf{h}_{t-1}}{\partial W_x})$$

- At each iteration backwards in time, the gradients are multiplied by W_h .
- If you search how $\frac{\partial \mathbf{h}_t}{\partial W_x}$ depends on \mathbf{x}_0 , you obtain something like:

$$\frac{\partial \mathbf{h}_t}{\partial W_x} \approx \prod_{k=0}^t \mathbf{h}'_k ((W_h)^t \mathbf{x}_0 + \dots)$$

- If $|W_h| > 1$, $|(W_h)^t|$ increases exponentially with t : the gradient **explodes**.
- If $|W_h| < 1$, $|(W_h)^t|$ decreases exponentially with t : the gradient **vanishes**.

Vanishing and exploding gradients

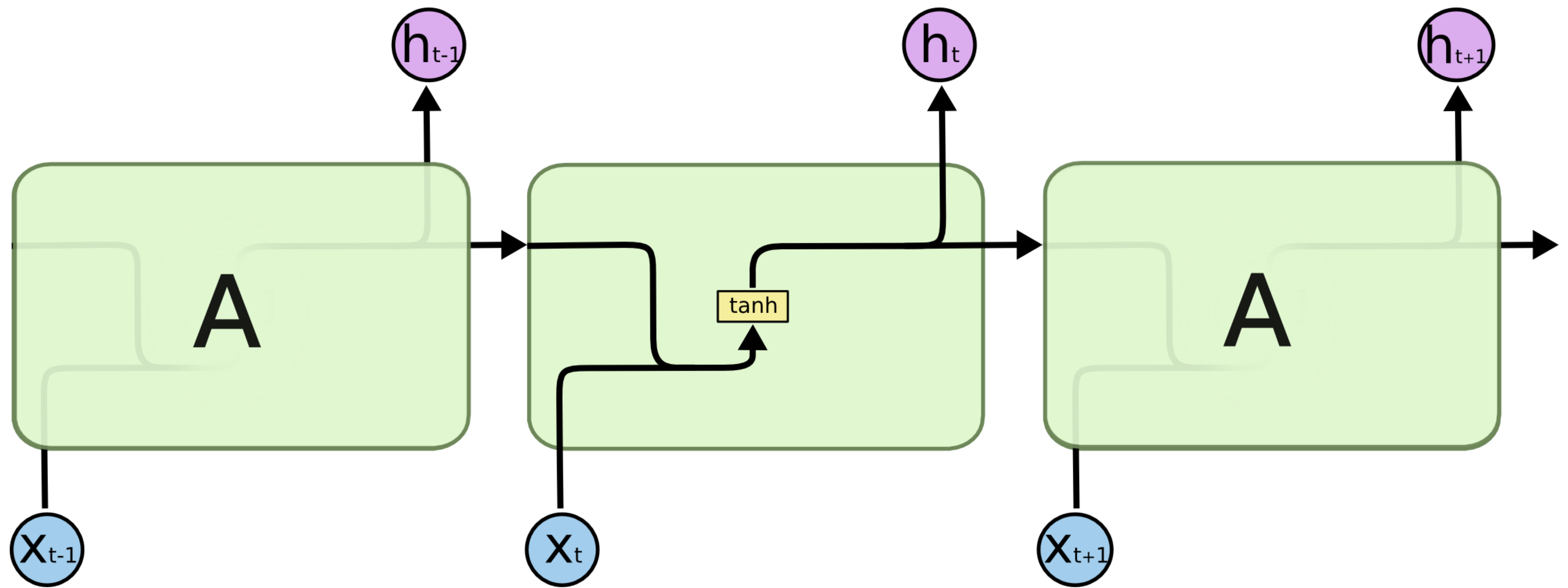
- **Exploding gradients** are relatively easy to deal with: one just clips the norm of the gradient to a maximal value.

$$\left\| \frac{\partial \mathcal{L}(W_x, W_h)}{\partial W_x} \right\| \leftarrow \min\left(\left\| \frac{\partial \mathcal{L}(W_x, W_h)}{\partial W_x} \right\|, T\right)$$

- But there is no solution to the **vanishing gradient problem** for regular RNNs: the gradient fades over time (backwards) and no long-term dependency can be learned.
- This is the same problem as for feedforward deep networks: a RNN is just a deep network rolled over itself.
- Its depth (number of layers) corresponds to the maximal number of steps back in time.
- In order to limit vanishing gradients and learn long-term dependencies, one has to use a more complex structure for the layer.
- This is the idea behind **long short-term memory** (LSTM) networks.

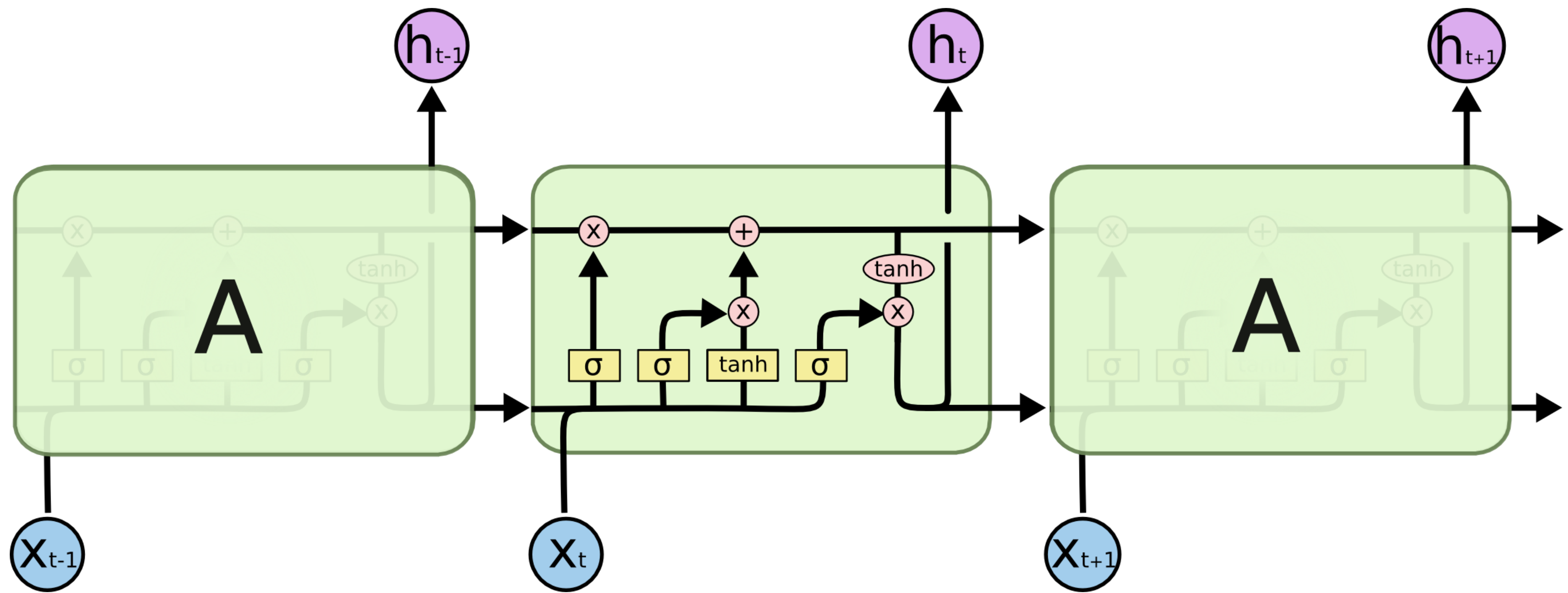
2 - LSTM

Regular RNN



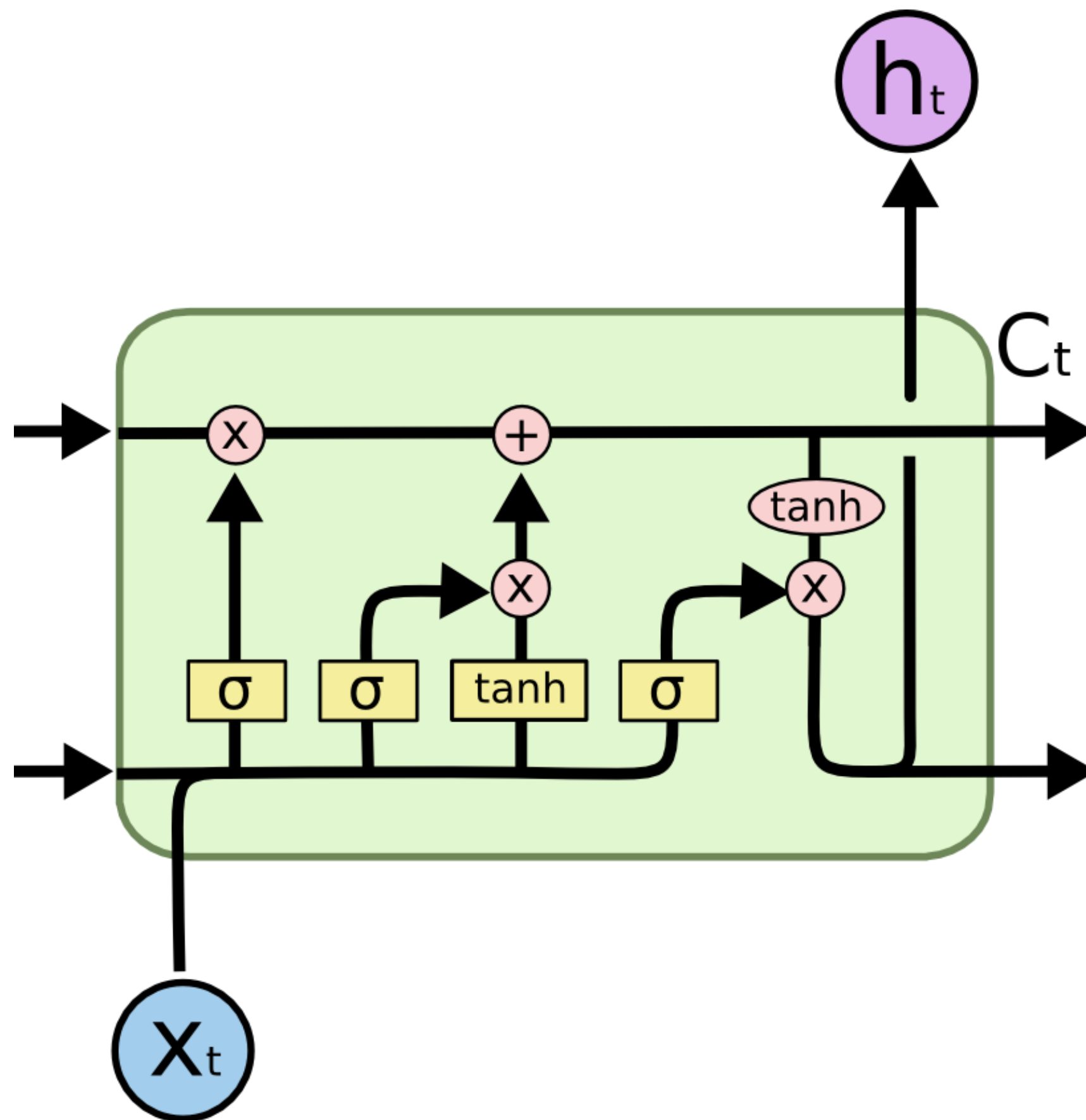
Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

LSTM



Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

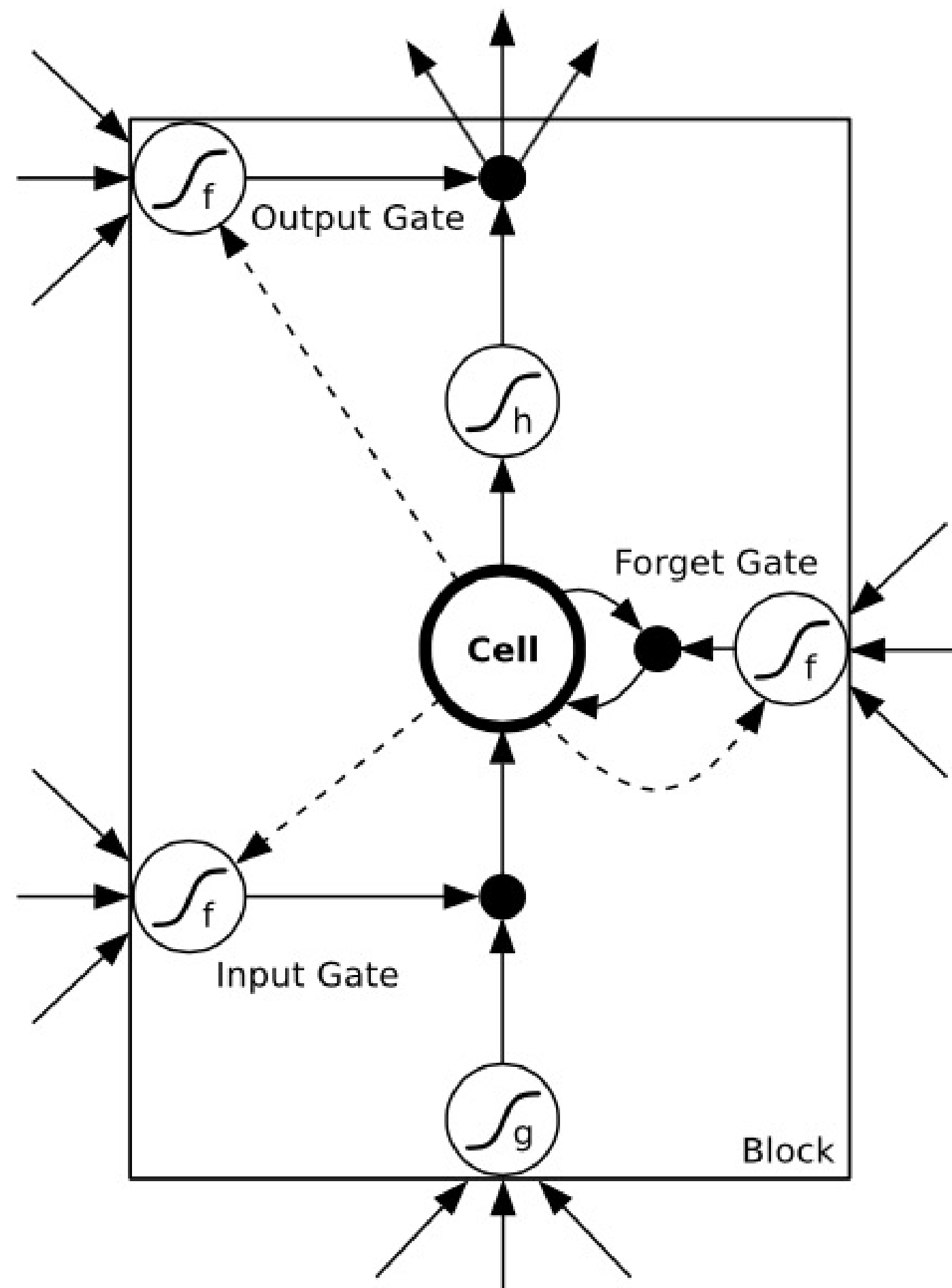
LSTM cell



- A **LSTM layer** is a RNN layer with the ability to control what it memorizes.
- In addition to the input x_t and output h_t , it also has a **state** C_t which is maintained over time.
- The state is the memory of the layer (sometimes called context).
- It also contains three multiplicative **gates**:
 - The **input gate** controls which inputs should enter the memory.
 - The **forget gate** controls which memory should be forgotten.
 - The **output gate** controls which part of the memory should be used to produce the output.

Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

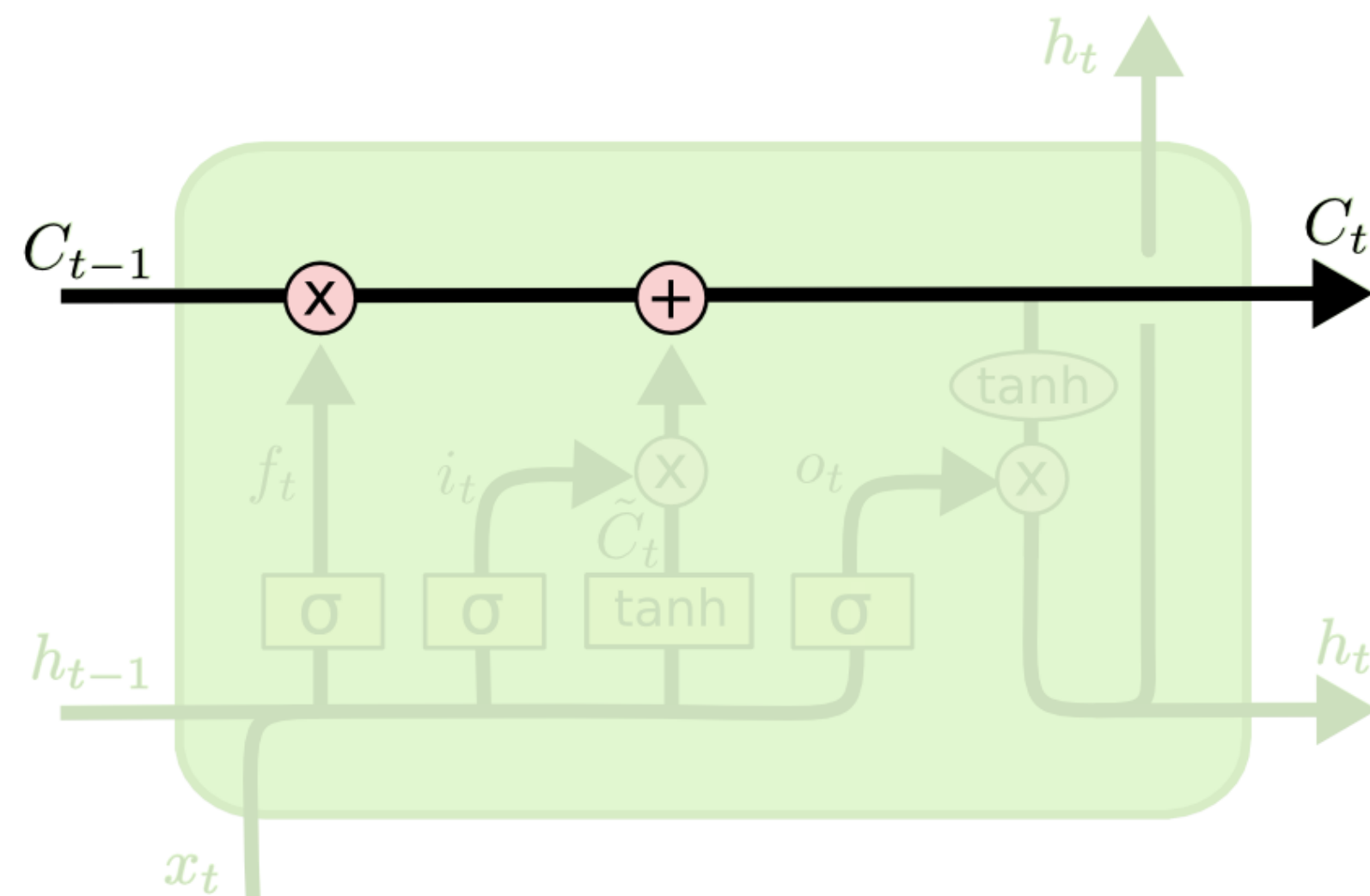
LSTM cell



- The **state** \mathbf{C}_t can be seen as an accumulator integrating inputs (and previous outputs) over time.
 - The **input gate** allows inputs to be stored.
 - *are they worth remembering?*
 - The **forget gate** “empties” the accumulator
 - *do I still need them?*
 - The **output gate** allows to use the accumulator for the output.
 - *should I respond now? Do I have enough information?*
- The gates **learn** to open and close through learnable weights.

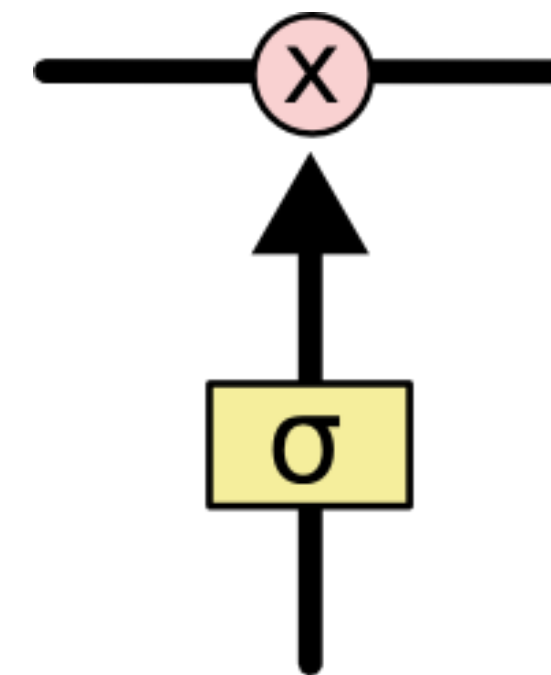
Source: <http://eric-yuan.me/rnn2-lstm/>

The cell state is propagated over time

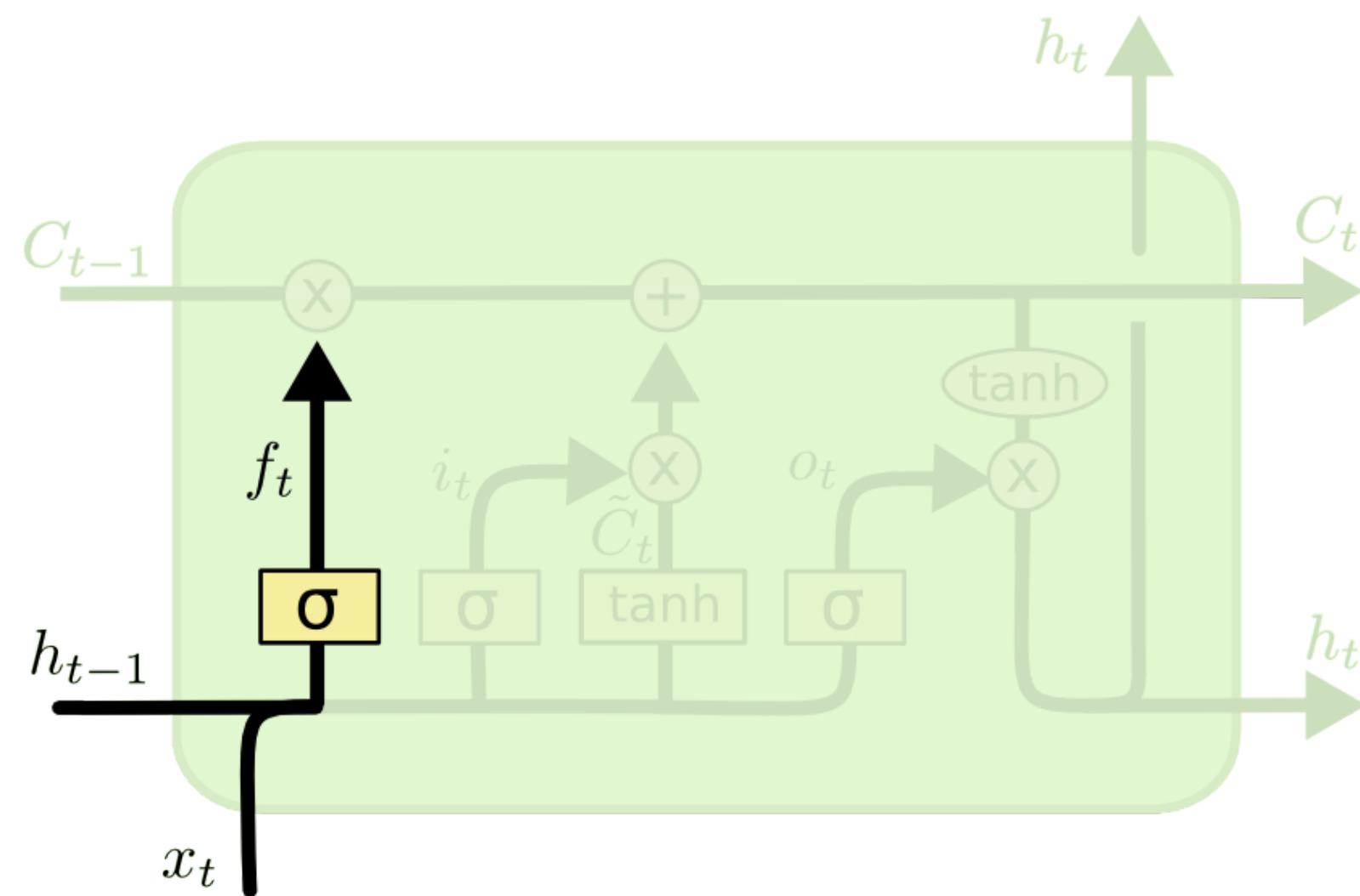


Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

- By default, the cell state C_t stays the same over time (*conveyor belt*).
- It can have the same number of dimensions as the output h_t , but does not have to.
- Its content can be erased by multiplying it with a vector of 0s, or preserved by multiplying it by a vector of 1s.
- We can use a **sigmoid** to achieve this:



The forget gate



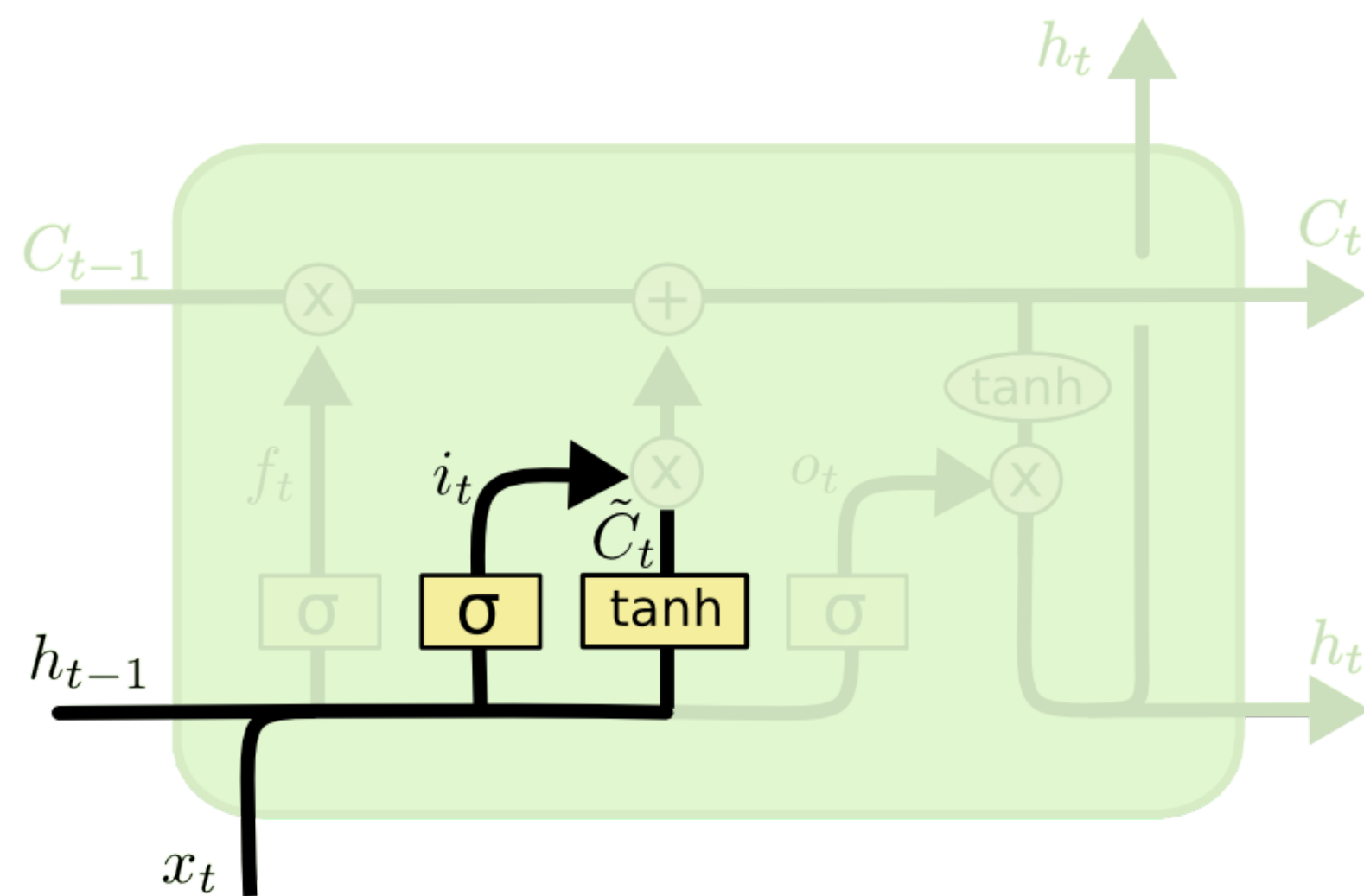
Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

- Forget weights W_f and a sigmoid function are used to decide if the state should be preserved or not.

$$\mathbf{f}_t = \sigma(W_f \times [\mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_f)$$

- $[\mathbf{h}_{t-1}; \mathbf{x}_t]$ is simply the concatenation of the two vectors \mathbf{h}_{t-1} and \mathbf{x}_t .
- \mathbf{f}_t is a vector of values between 0 and 1, one per dimension of the cell state \mathbf{C}_t .

The input gate



Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

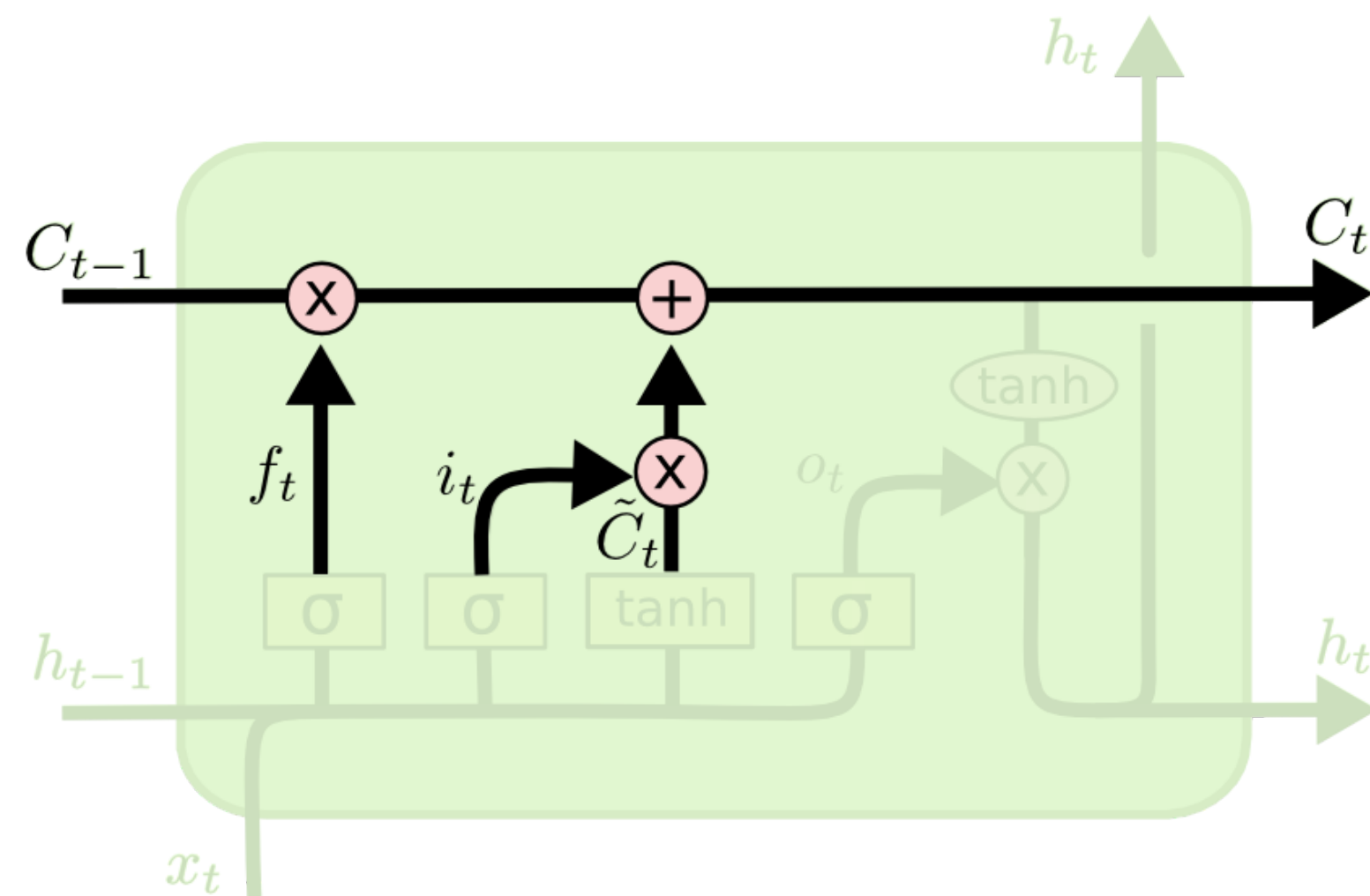
- Similarly, the input gate uses a sigmoid function to decide if the state should be updated or not.

$$\mathbf{i}_t = \sigma(W_i \times [\mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_i)$$

- As for RNNs, the input \mathbf{x}_t and previous output \mathbf{h}_{t-1} are combined to produce a **candidate state** $\tilde{\mathbf{C}}_t$ using the tanh transfer function.

$$\tilde{\mathbf{C}}_t = \tanh(W_C \times [\mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_c)$$

Updating the state



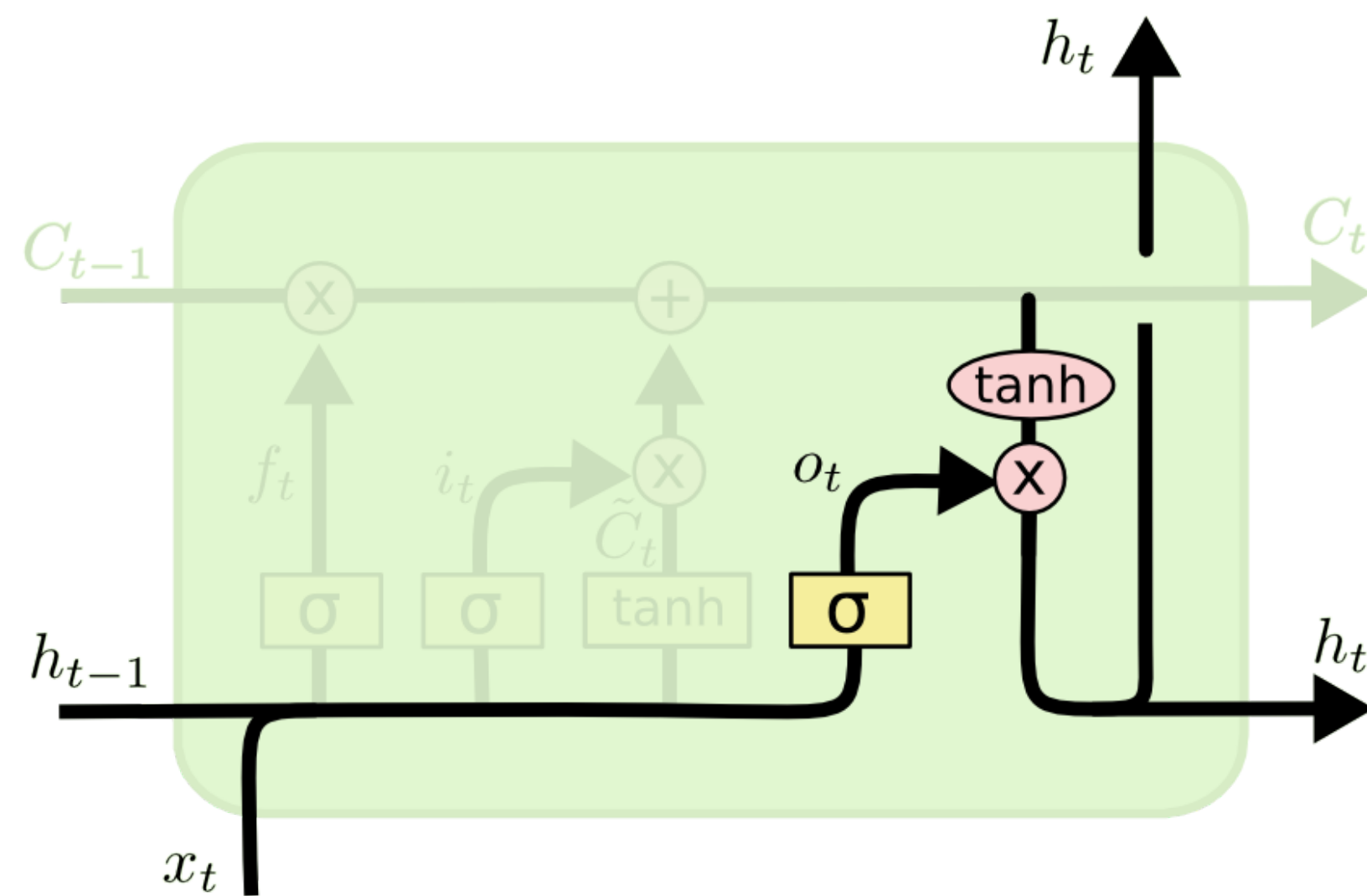
Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

- The new state \mathbf{C}_t is computed as a part of the previous state \mathbf{C}_{t-1} (element-wise multiplication with the forget gate \mathbf{f}_t) plus a part of the candidate state $\tilde{\mathbf{C}}_t$ (element-wise multiplication with the input gate \mathbf{i}_t).

$$\mathbf{C}_t = \mathbf{f}_t \odot \mathbf{C}_{t-1} + \mathbf{i}_t \odot \tilde{\mathbf{C}}_t$$

- Depending on the gates, the new state can be equal to the previous state (gates closed), the candidate state (gates opened) or a mixture of both.

The output gate



- The output gate decides which part of the new state will be used for the output.
- The output not only influences the decision, but also how the gates will be updated at the next step.

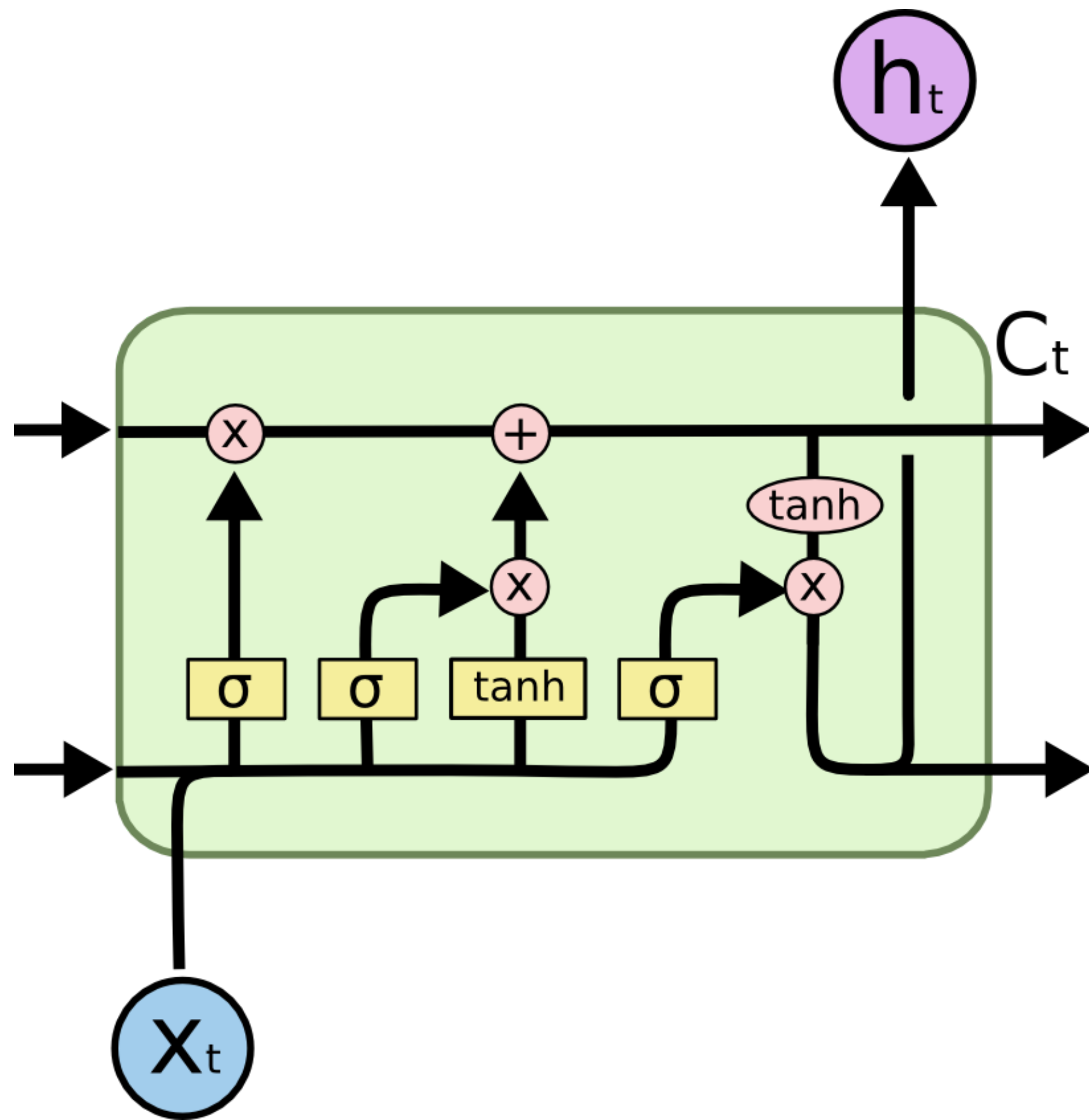
$$\mathbf{o}_t = \sigma(W_o \times [\mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_o)$$

$$\mathbf{h}_t = \mathbf{o}_t \odot \tanh(\mathbf{C}_t)$$

Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

LSTM

- The function between \mathbf{x}_t and \mathbf{h}_t is quite complicated, with many different weights, but everything is differentiable: BPTT can be applied.



Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

Forget gate

$$\mathbf{f}_t = \sigma(W_f \times [\mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_f)$$

Input gate

$$\mathbf{i}_t = \sigma(W_i \times [\mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_i)$$

Output gate

$$\mathbf{o}_t = \sigma(W_o \times [\mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_o)$$

Candidate state

$$\tilde{\mathbf{C}}_t = \tanh(W_C \times [\mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_c)$$

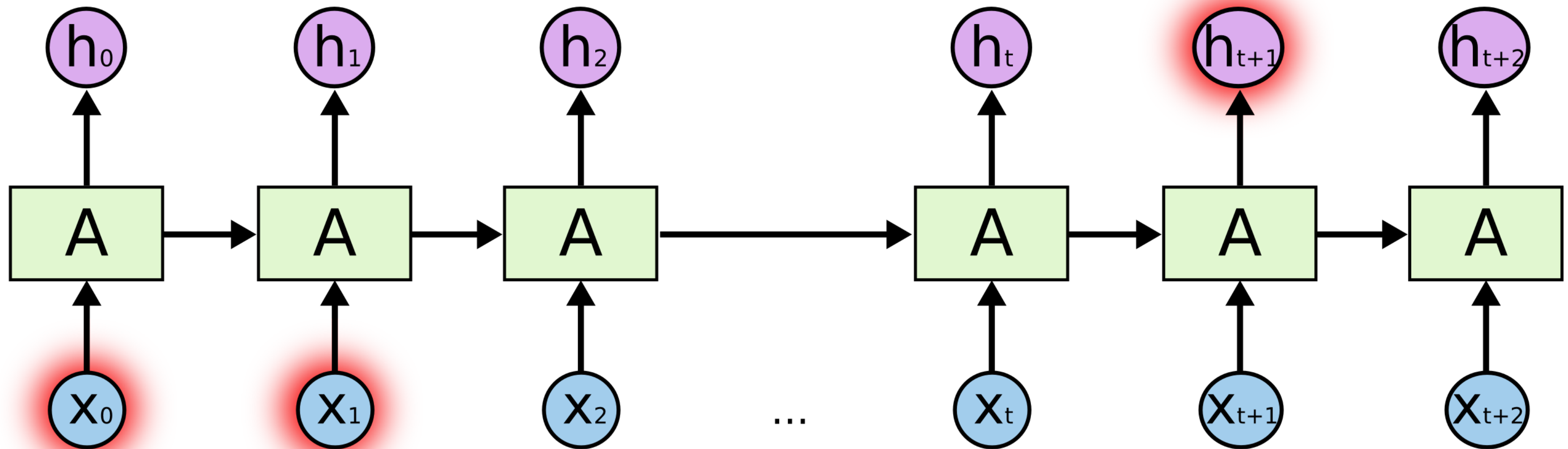
New state

$$\mathbf{C}_t = \mathbf{f}_t \odot \mathbf{C}_{t-1} + \mathbf{i}_t \odot \tilde{\mathbf{C}}_t$$

Output

$$\mathbf{h}_t = \mathbf{o}_t \odot \tanh(\mathbf{C}_t)$$

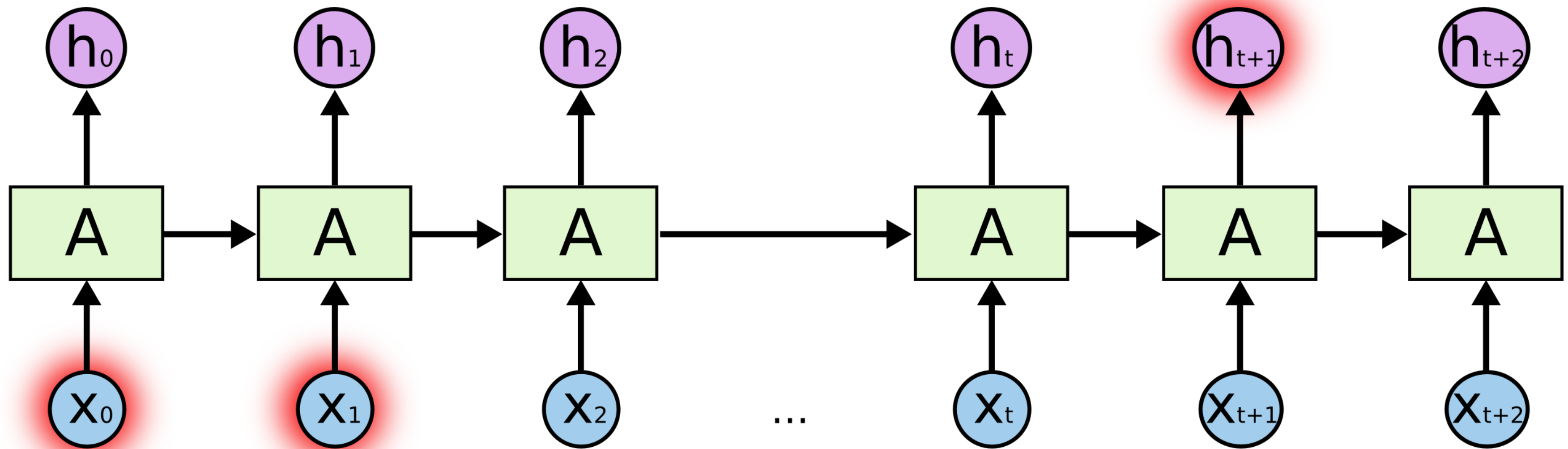
How do LSTM solve the vanishing gradient problem?



Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

- Not all inputs are remembered by the LSTM: the input gate controls what comes in.
- If only x_0 and x_1 are needed to produce h_{t+1} , they will be the only ones stored in the state, the other inputs are ignored.

How do LSTM solve the vanishing gradient problem?



Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

- If the state stays constant between $t = 1$ and t , the gradient of the error will not vanish when backpropagating from t to $t = 1$, because nothing happens!

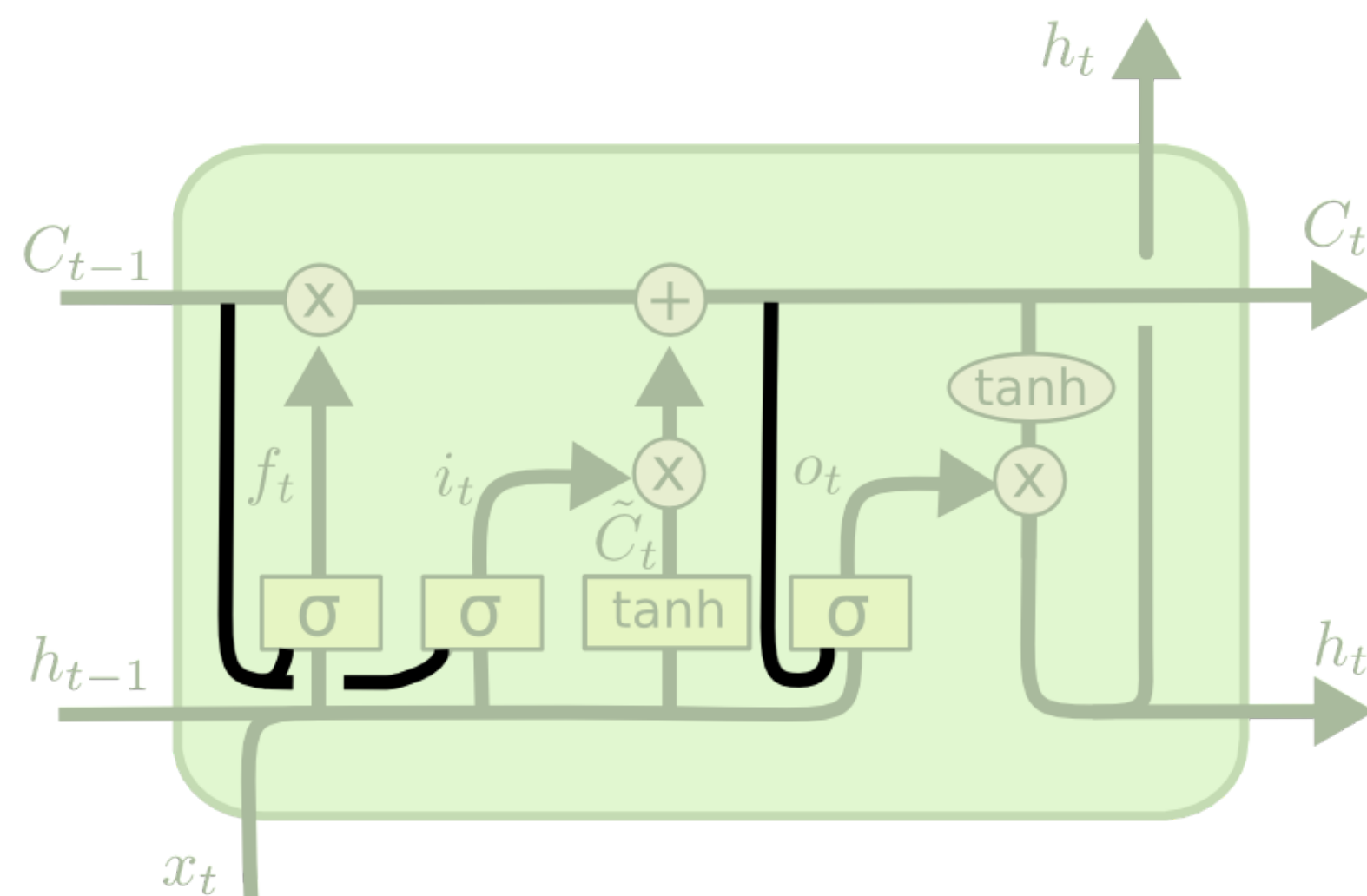
$$\mathbf{C}_t = \mathbf{C}_{t-1} \rightarrow \frac{\partial \mathbf{C}_t}{\partial \mathbf{C}_{t-1}} = 1$$

- The gradient is multiplied by exactly one when the gates are closed.

LSTM networks

- LSTM are particularly good at learning long-term dependencies, because the gates protect the cell from vanishing gradients.
- Its problem is how to find out which inputs (e.g. \mathbf{x}_0 and \mathbf{x}_1) should enter or leave the state memory.
- Truncated BPTT is used to train all weights: the weights for the candidate state (as for RNN), and the weights of the three gates.
- LSTM are also subject to overfitting. Regularization (including dropout) can be used.
- The weights (also for the gates) can be convolutional.
- The gates also have a bias, which can be fixed (but hard to find).
- LSTM layers can be stacked to detect dependencies at different scales (deep LSTM network).

Peephole connections



Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

- A popular variant of LSTM adds *peephole* connections, where the three gates have additionally access to the state \mathbf{C}_{t-1} .

$$\mathbf{f}_t = \sigma(W_f \times [\mathbf{C}_{t-1}; \mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_f)$$

$$\mathbf{i}_t = \sigma(W_i \times [\mathbf{C}_{t-1}; \mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_i)$$

$$\mathbf{o}_t = \sigma(W_o \times [\mathbf{C}_t; \mathbf{h}_{t-1}; \mathbf{x}_t] + \mathbf{b}_o)$$

- It usually works better, but it adds more weights.

GRU: Gated Recurrent Unit

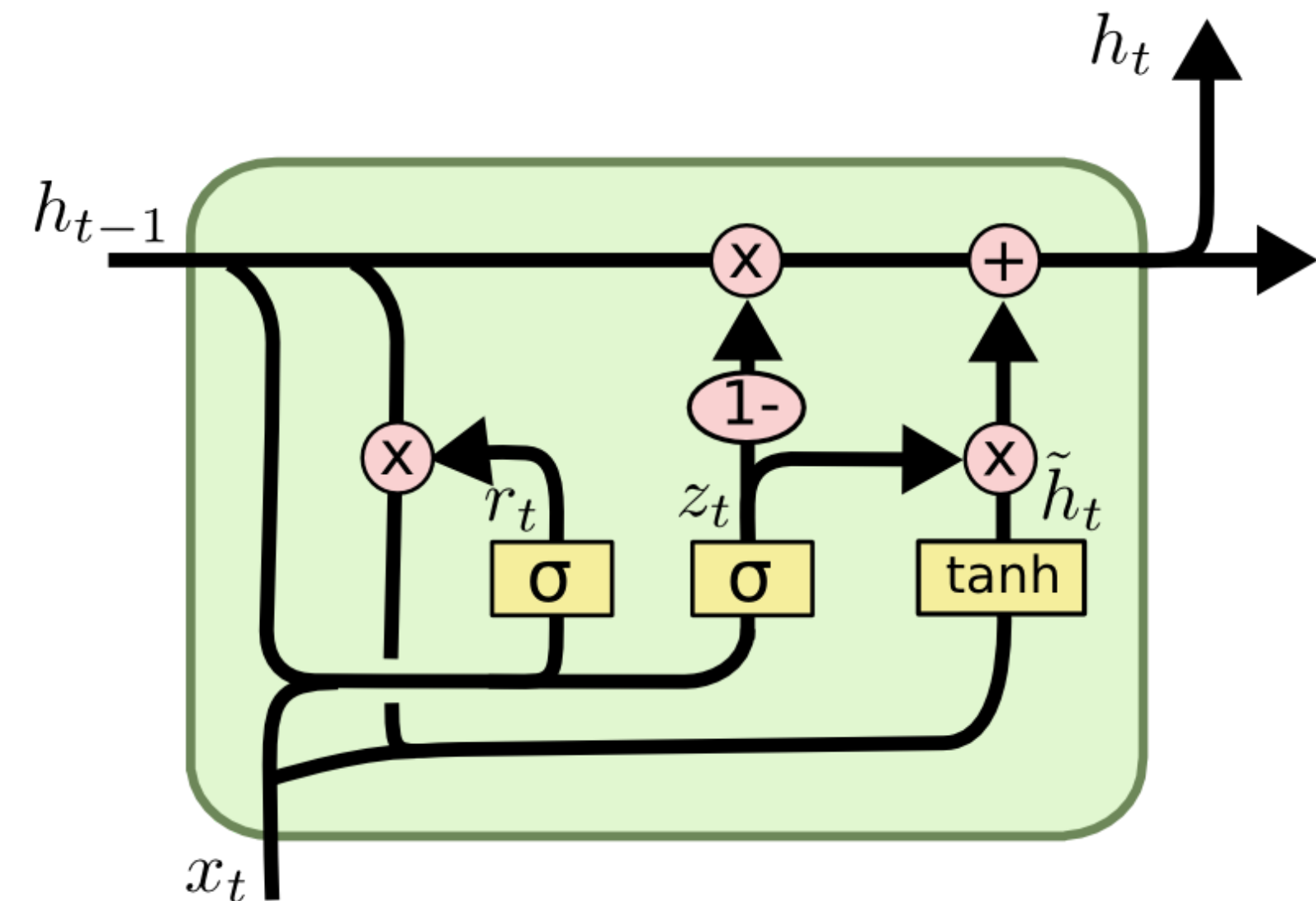
- Another variant is called the **Gated Recurrent Unit (GRU)**.
- It uses directly the output \mathbf{h}_t as a state, and the forget and input gates are merged into a single gate \mathbf{r}_t .

$$\mathbf{z}_t = \sigma(W_z \times [\mathbf{h}_{t-1}; \mathbf{x}_t])$$

$$\mathbf{r}_t = \sigma(W_r \times [\mathbf{h}_{t-1}; \mathbf{x}_t])$$

$$\tilde{\mathbf{h}}_t = \tanh(W_h \times [\mathbf{r}_t \odot \mathbf{h}_{t-1}; \mathbf{x}_t])$$

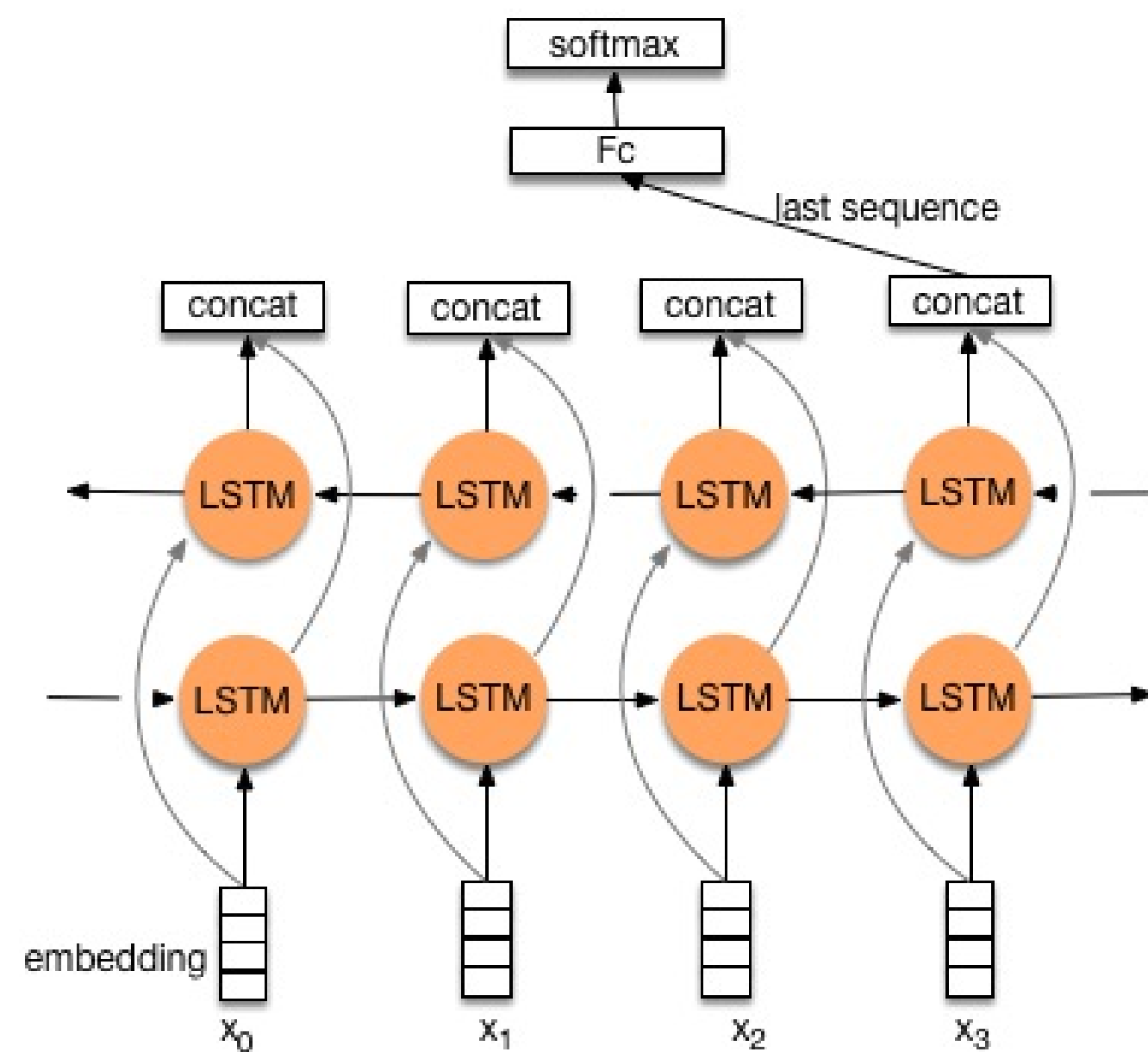
$$\mathbf{h}_t = (1 - \mathbf{z}_t) \odot \mathbf{h}_{t-1} + \mathbf{z}_t \odot \tilde{\mathbf{h}}_t$$



Source: <http://colah.github.io/posts/2015-08-Understanding-LSTMs>

- It does not even need biases (mostly useless in LSTMs anyway).
- Much simpler to train as the LSTM, and almost as powerful.

Bidirectional LSTM



- A **bidirectional LSTM** learns to predict the output in two directions:
 - The **feedforward** line learns using the past context (classical LSTM).
 - The **backforward** line learns using the future context (inputs are reversed).
- The two state vectors are then concatenated at each time step to produce the output.
- Only possible offline, as the future inputs must be known.
- Works better than LSTM on many problems, but slower.

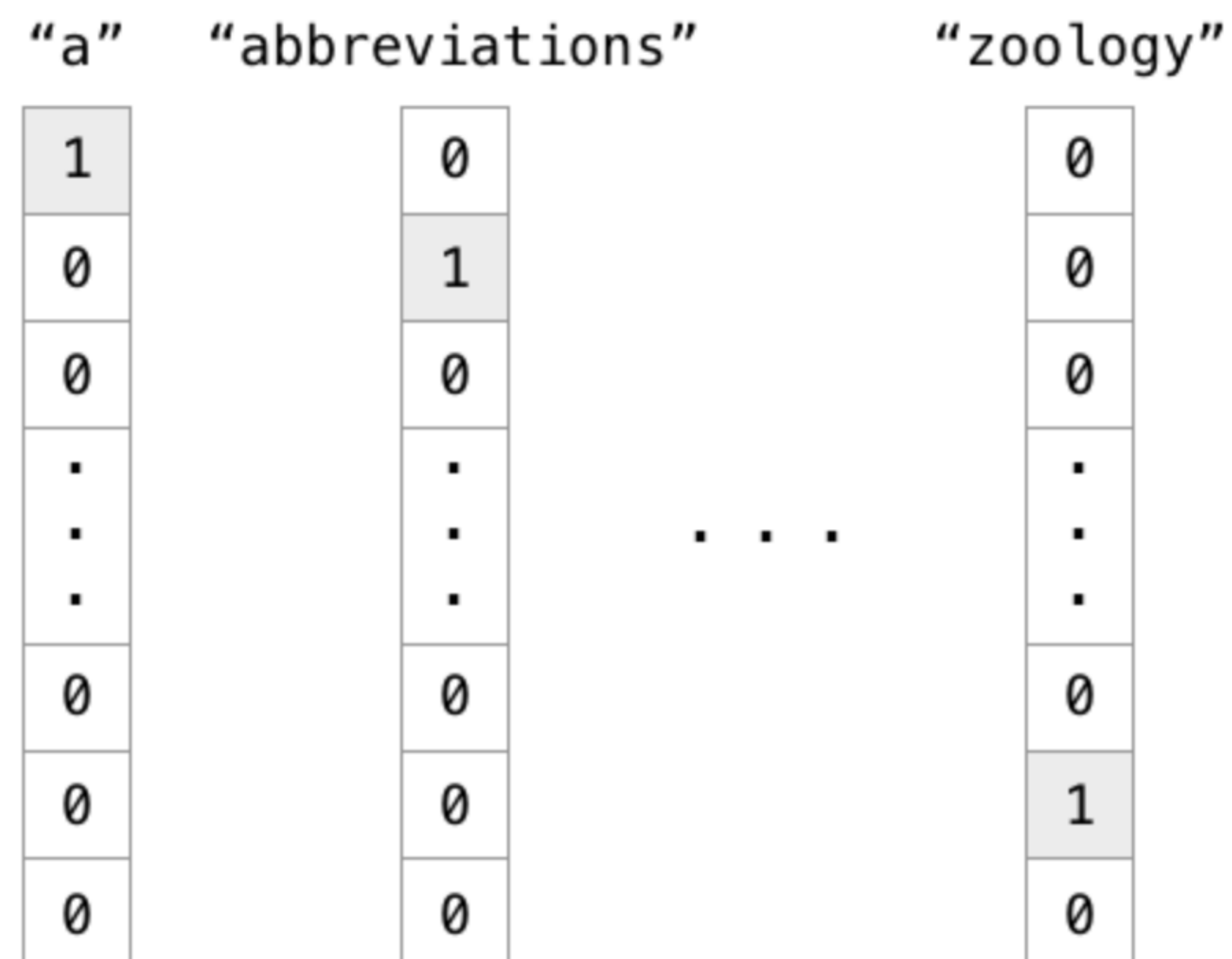
Source:

http://www.paddlepaddle.org/doc/demo/sentiment_analysis/sentiment_analysis.html

3 - word2vec

Representing words

- The most famous application of RNNs is **Natural Language Processing** (NLP): text understanding, translation, etc...
- Each word of a sentence has to be represented as a vector \mathbf{x}_t in order to be fed to a LSTM.
- Which representation should we use?
- The naive solution is to use **one-hot encoding**, one element of the vector corresponding to one word of the dictionary.

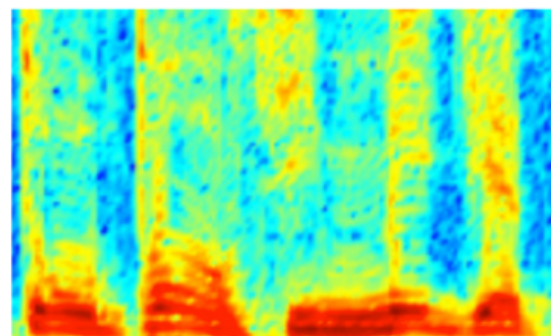


Source: https://cdn-images-1.medium.com/max/1600/1*ULfyiWPKgWceCqyZeDTI0g.png

Representing words

- One-hot encoding is not a good representation for words:
 - The vector size will depend on the number of words of the language:
 - English: 171,476 (Oxford English Dictionary), 470,000 (Merriam-Webster)... 20,000 in practice.
 - French: 270,000 (TILF).
 - German: 200,000 (Duden).
 - Chinese: 370,000 (Hanyu Da Cidian).
 - Korean: 1,100,373 (Woori Mal Saem)
 - Semantically related words have completely different representations (“endure” and “tolerate”).
 - The representation is extremely **sparse** (a lot of useless zeros).

AUDIO



Audio Spectrogram

DENSE

IMAGES

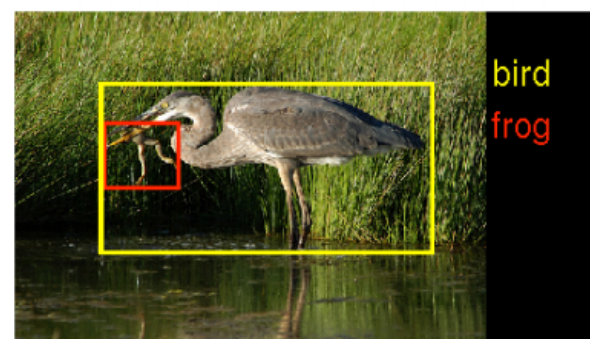
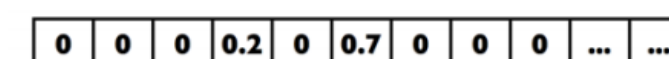


Image pixels

DENSE

TEXT



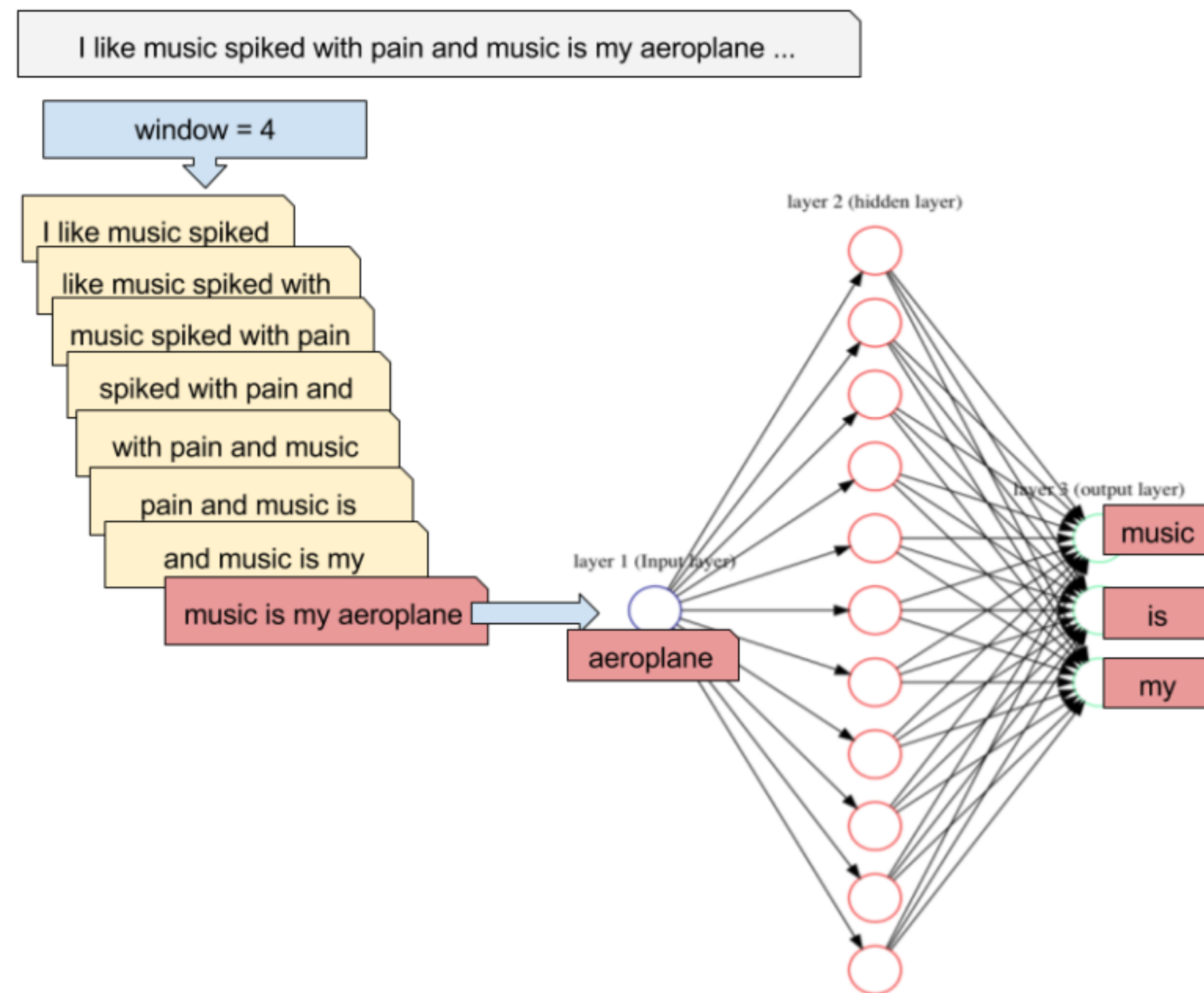
Word, context, or document vectors

SPARSE

Source: <https://www.tensorflow.org/tutorials/representation/word2vec>

word2vec

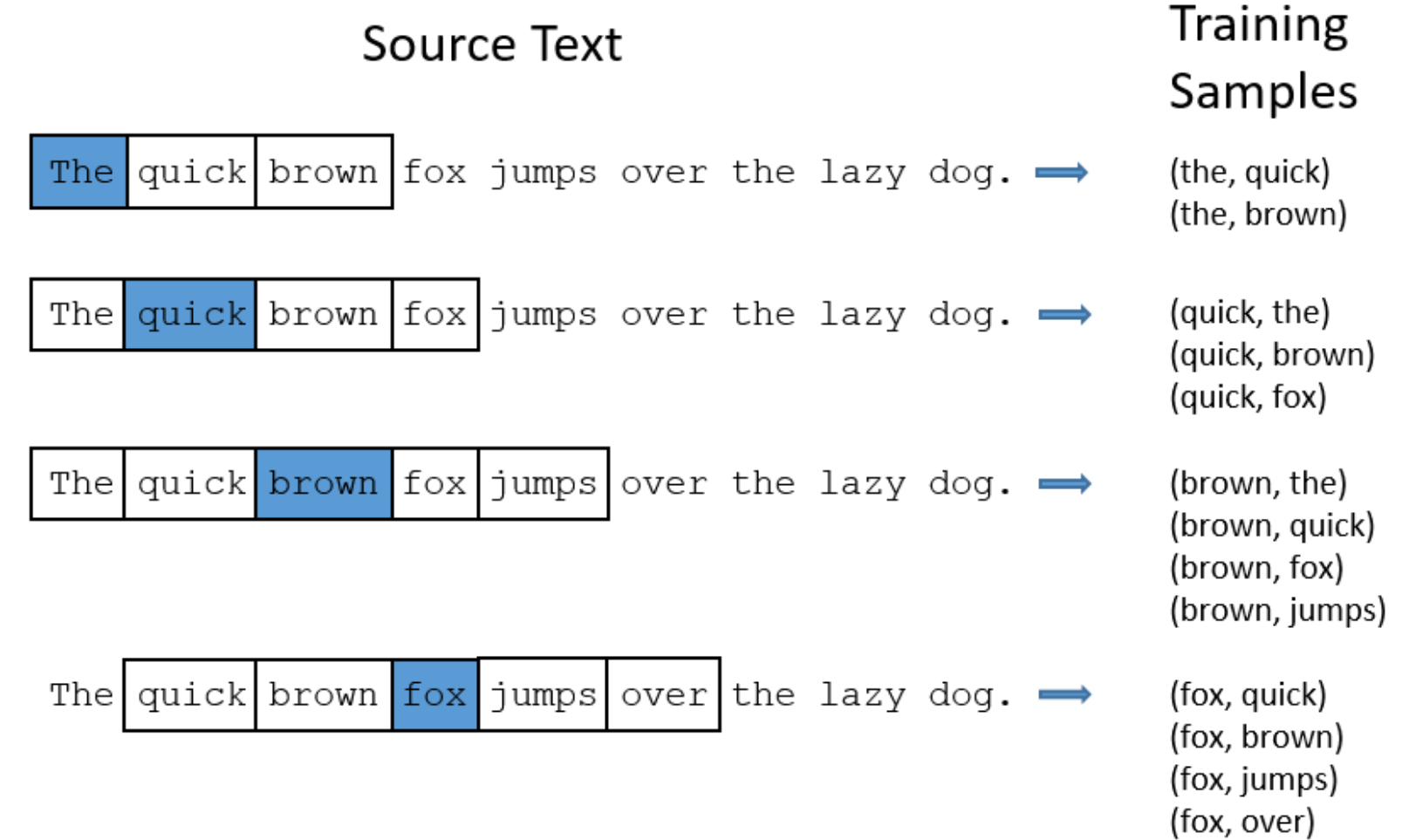
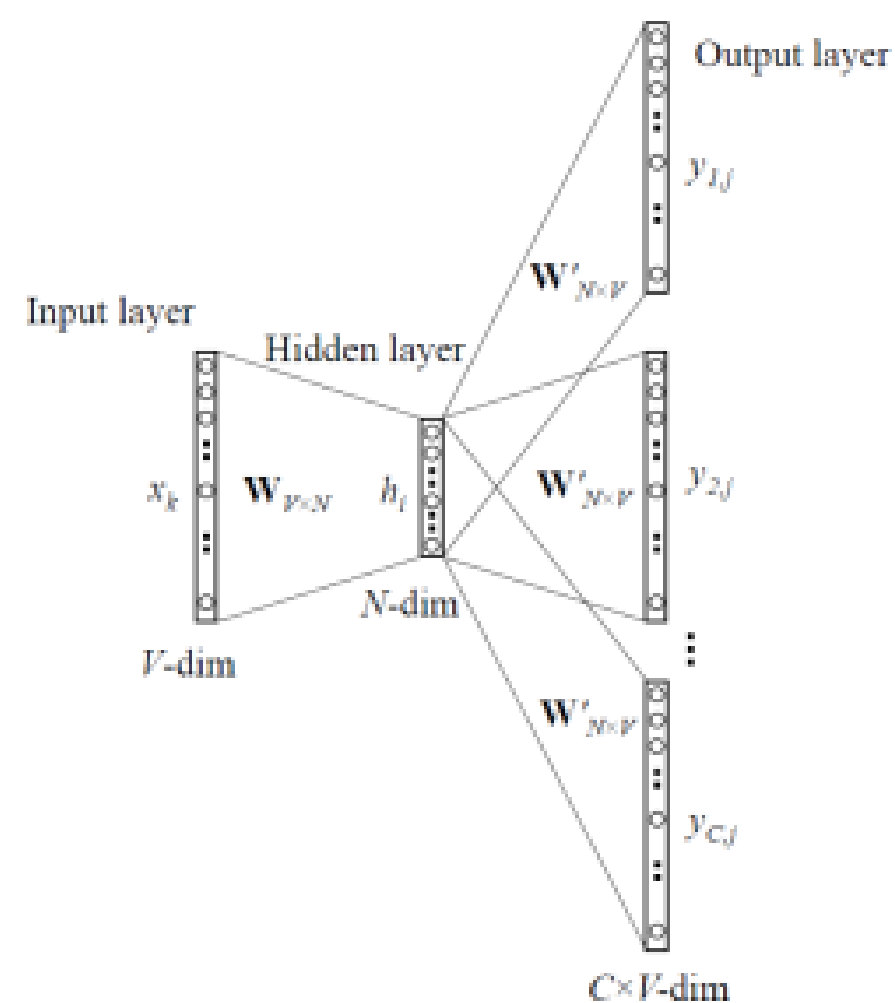
- **word2vec** learns word **embeddings** by trying to predict the current word based on the context (CBOW, continuous bag-of-words) or the context based on the current word (skip-gram).
- It uses a three-layer autoencoder-like NN, where the hidden layer (latent space) will learn to represent the one-hot encoded words in a dense manner.



Source: <https://jaxenter.com/deep-learning-search-word2vec-147782.html>

word2vec

- **word2vec** has three parameters:
 - the **vocabulary size**: number of words in the dictionary.
 - the **embedding size**: number of neurons in the hidden layer.
 - the **context size**: number of surrounding words to predict.
- It is trained on huge datasets of sentences (e.g. Wikipedia).

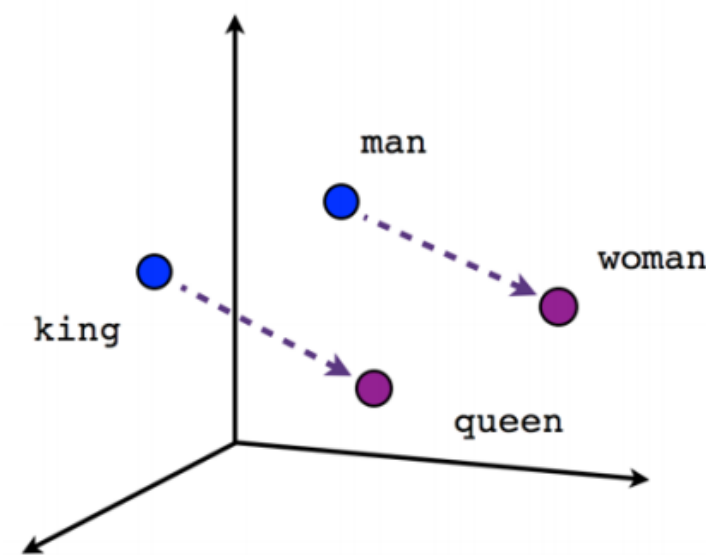


Source: <https://www.analyticsvidhya.com/blog/2017/06/word-embeddings-count-word2veec/>

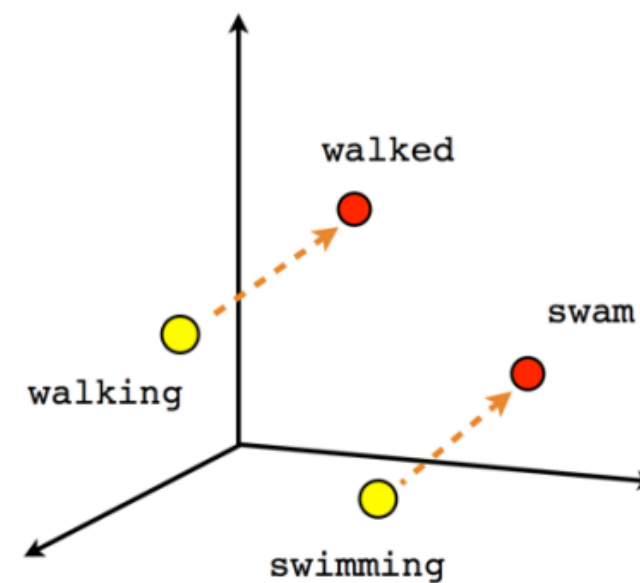
word2vec

- After learning, the hidden layer represents an **embedding vector**, which is a dense and compressed representation of each possible word (dimensionality reduction).
- Semantically close words (“endure” and “tolerate”) tend to appear in similar contexts, so their embedded representations will be close (Euclidian distance).
- One can even perform arithmetic operations on these vectors!

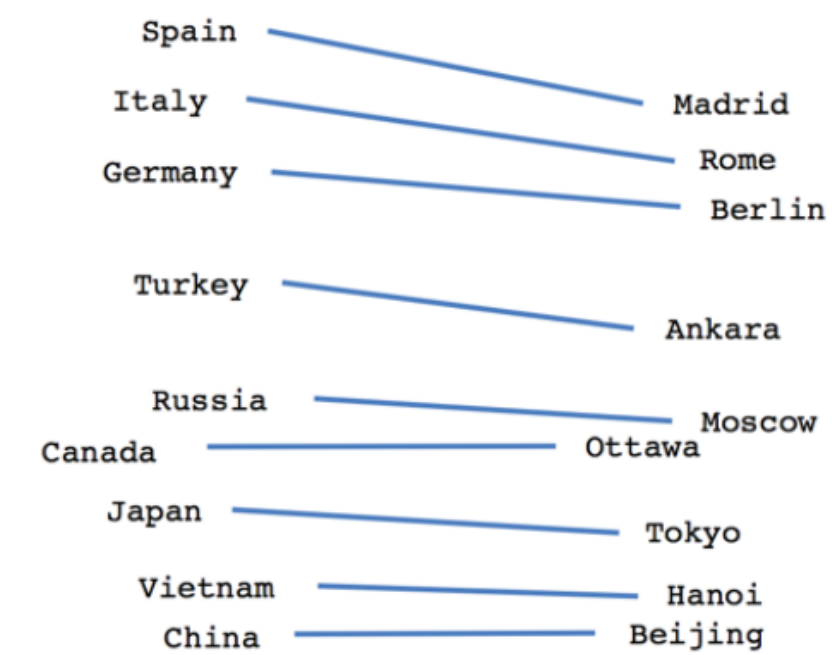
queen = king + woman - man



Male-Female



Verb tense

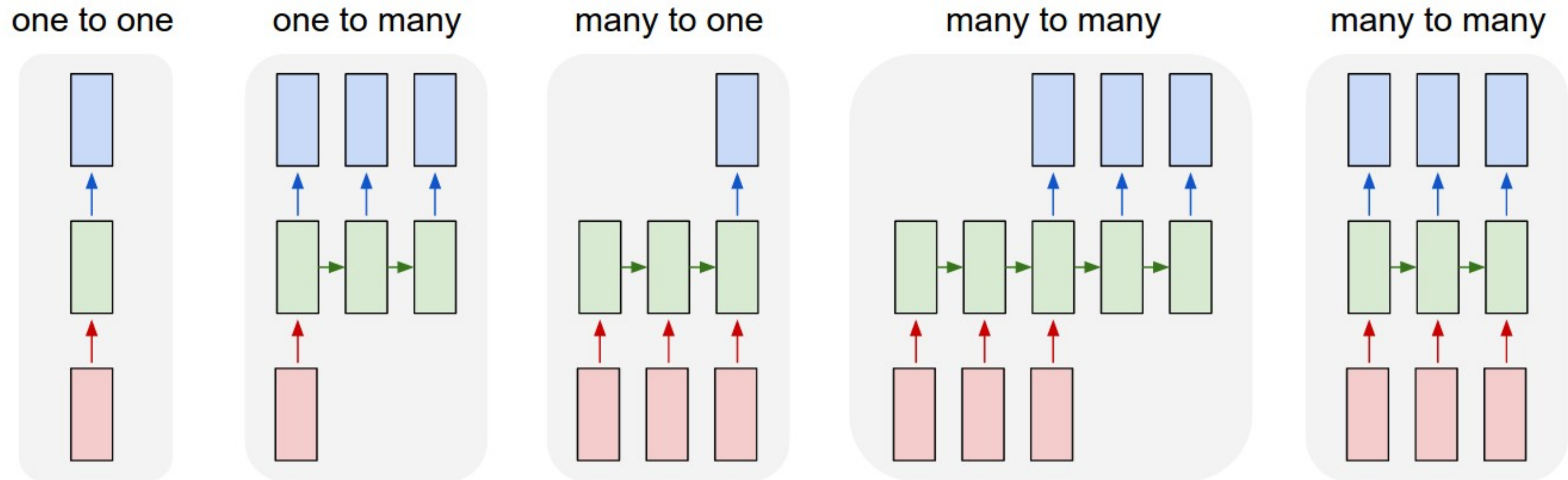


Country-Capital

Source : <https://www.tensorflow.org/tutorials/representation/word2vec>

4 - Applications of RNNs

Classification of LSTM architectures

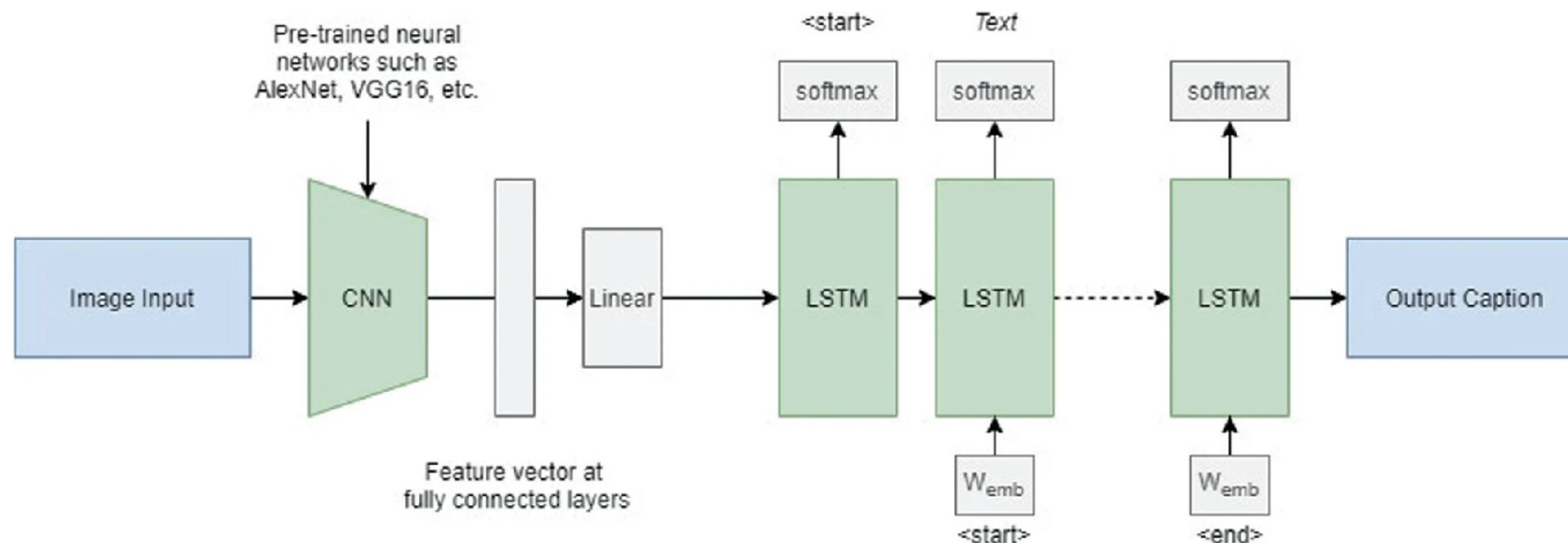


Source: <http://karpathy.github.io/2015/05/21/rnn-effectiveness/>

- **One to One:** classical feedforward network.
Image \rightarrow Label.
- **One to Many:** single input, many outputs.
Image \rightarrow Text.
- **Many to One:** sequence of inputs, single output.
Video / Text \rightarrow Label.
- **Many to Many:** sequence to sequence.
Text \rightarrow Text.
Video \rightarrow Text.

One to Many: image caption generation

- **Show and Tell** uses the last FC layer of a CNN to feed a LSTM layer and generate words.
- The pretrained CNN (VGG16, ResNet50) is used as a **feature extractor**.



Source: Sathe et al. (2022). Overview of Image Caption Generators and Its Applications. ICCSA. https://doi.org/10.1007/978-981-19-0863-7_8

- Each word of the sentence is encoded/decoded using word2vec.
- The output of the LSTM at time t becomes its new input at time $t + 1$.

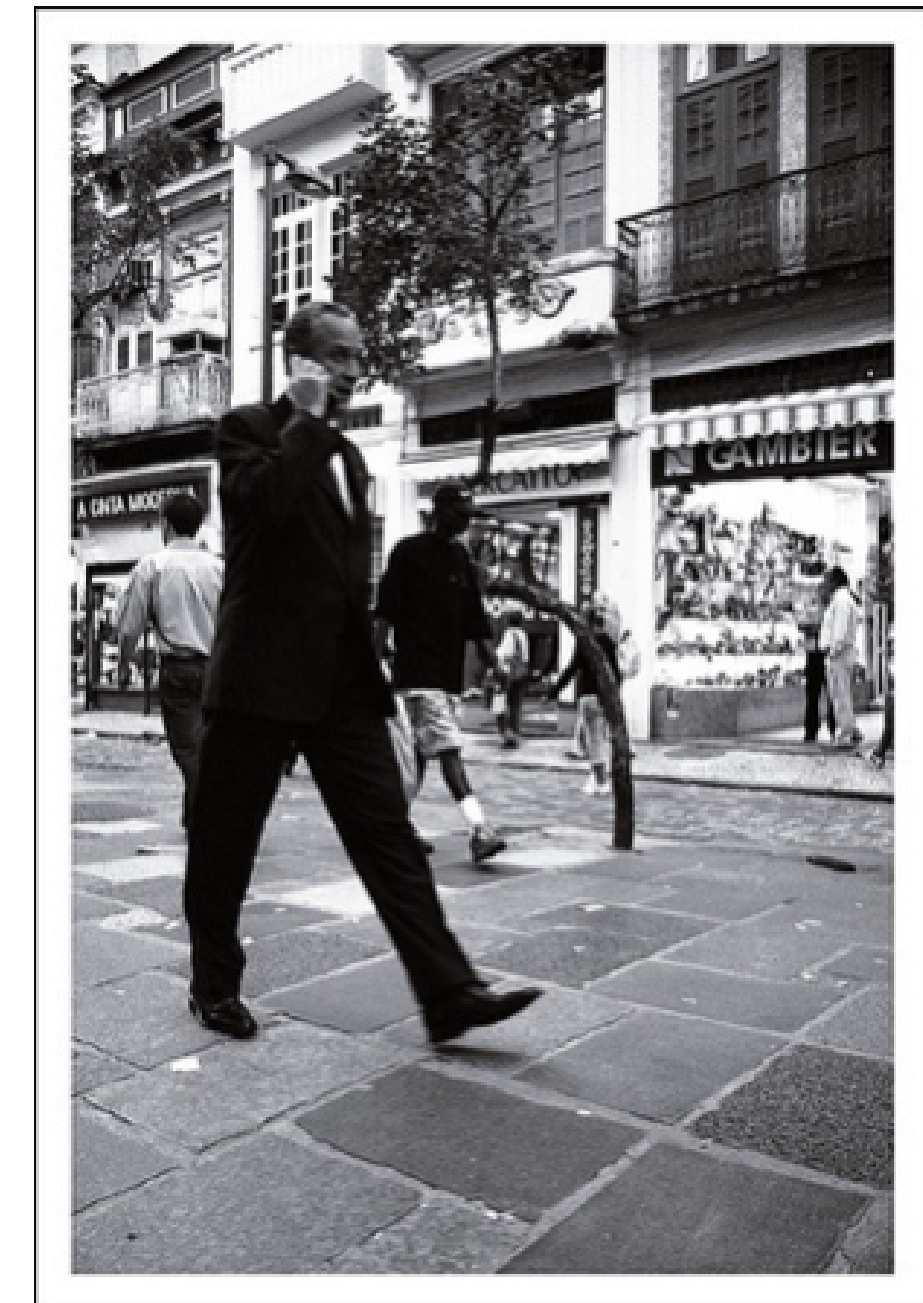
One to Many: image caption generation



↑ a living room with a couch and a television



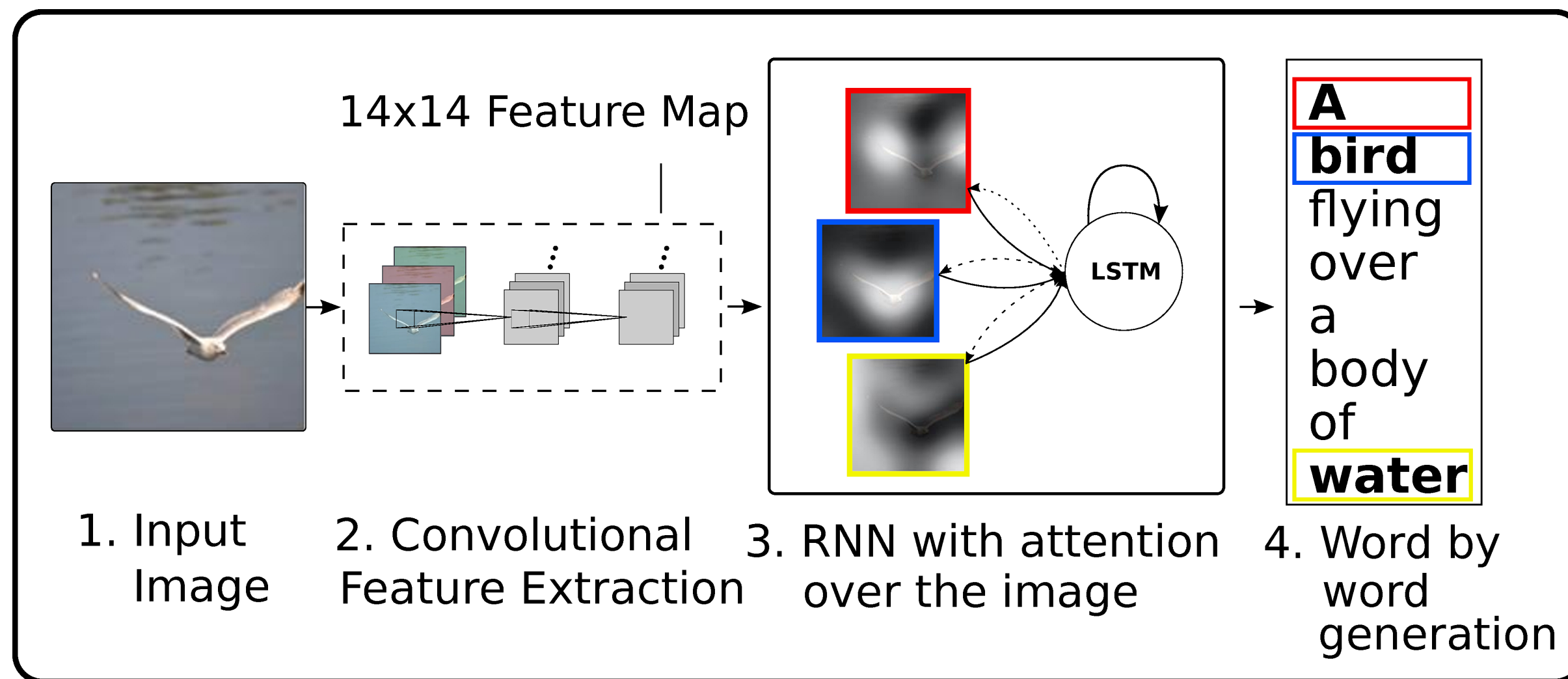
↑ a man riding a bike on a beach



a man is walking down the street with a suitcase ↗

One to Many: image caption generation

- **Show, attend and tell** uses attention to focus on specific parts of the image when generating the sentence.

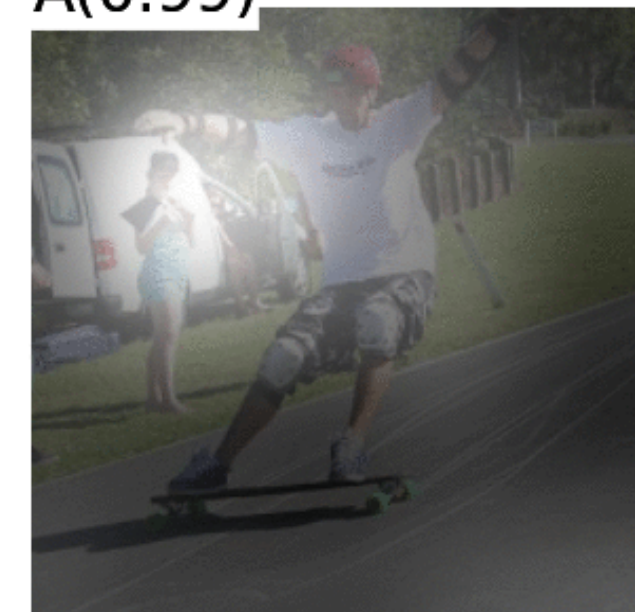


Source: <http://kelvinxu.github.io/projects/capgen.html>

A(0.91)



A(0.99)



Many to One: next character/word prediction

PANDARUS:

Alas, I think he shall be come approached and
the day
When little srain would be attain'd into being
never fed,
And who is but a chain and subjects of his
death,
I should not sleep.

Second Senator:

They are away this miseries, produced upon my
soul,
Breaking and strongly should be buried, when I
perish
The earth and thoughts of many states.

DUKE VINCENTIO:

Well, your wit is in the care of side and that.

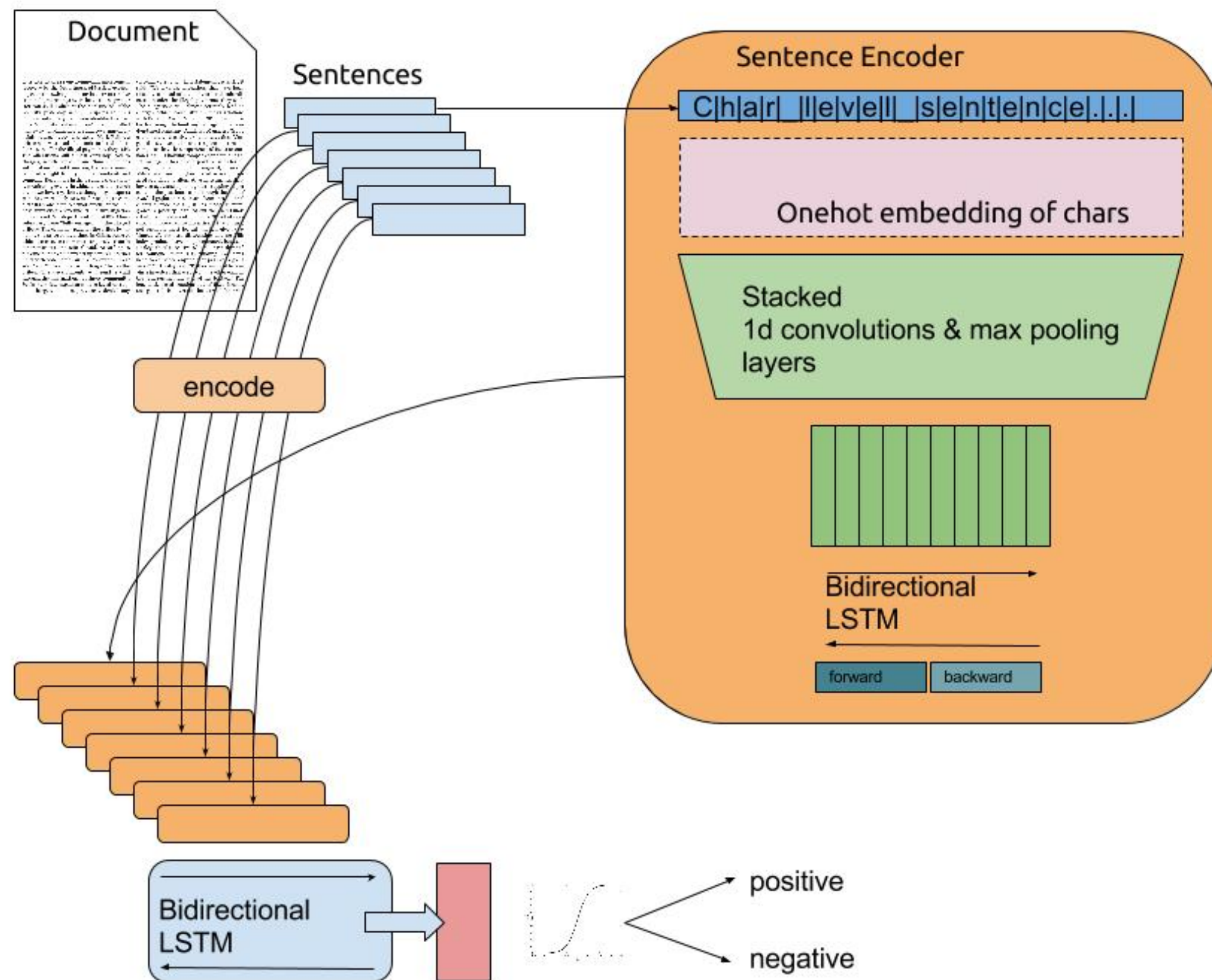
- Characters or words are fed one by one into a LSTM.
- The desired output is the next character or word in the text.
- Example:
 - Inputs: **To, be, or, not, to**
 - Output: **be**
- The text on the left was generated by a LSTM having read the entire writings of William Shakespeare.
- Each generated word is used as the next input.

Many to one: Sunspring SciFi movie



More info: <http://www.thereforefilms.com/sunspring.html>

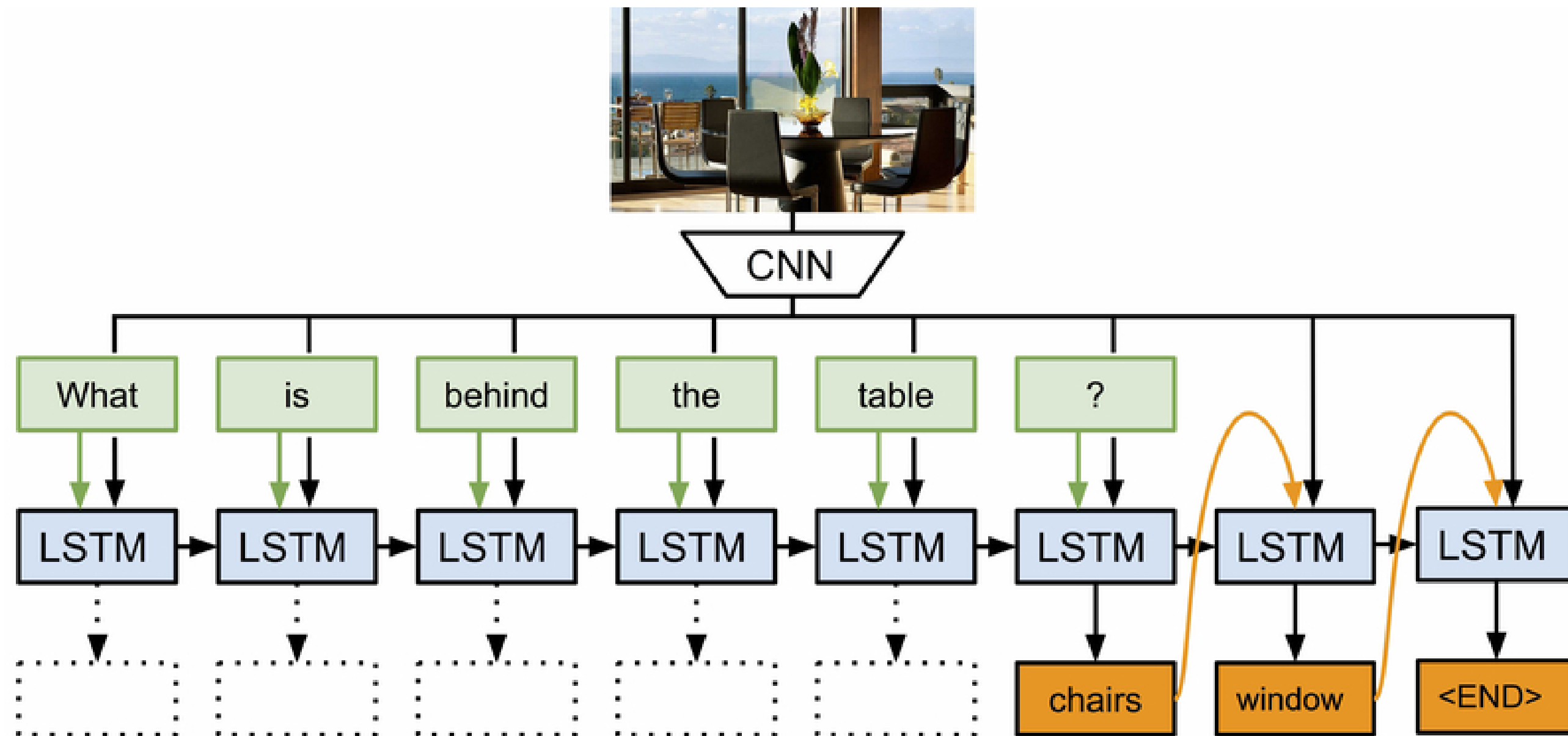
Many to One: sentiment analysis



- To obtain a vector from a sentence, **one-hot encoding** is used (alternative: word2vec).
- A 1D convolutional layers “slides” over the text.
- The bidirectional LSTM computes a state vector for the complete text.
- A classifier (fully connected layer) learns to predict the sentiment of the text (positive/negative).

Source: <https://offbit.github.io/how-to-read/>

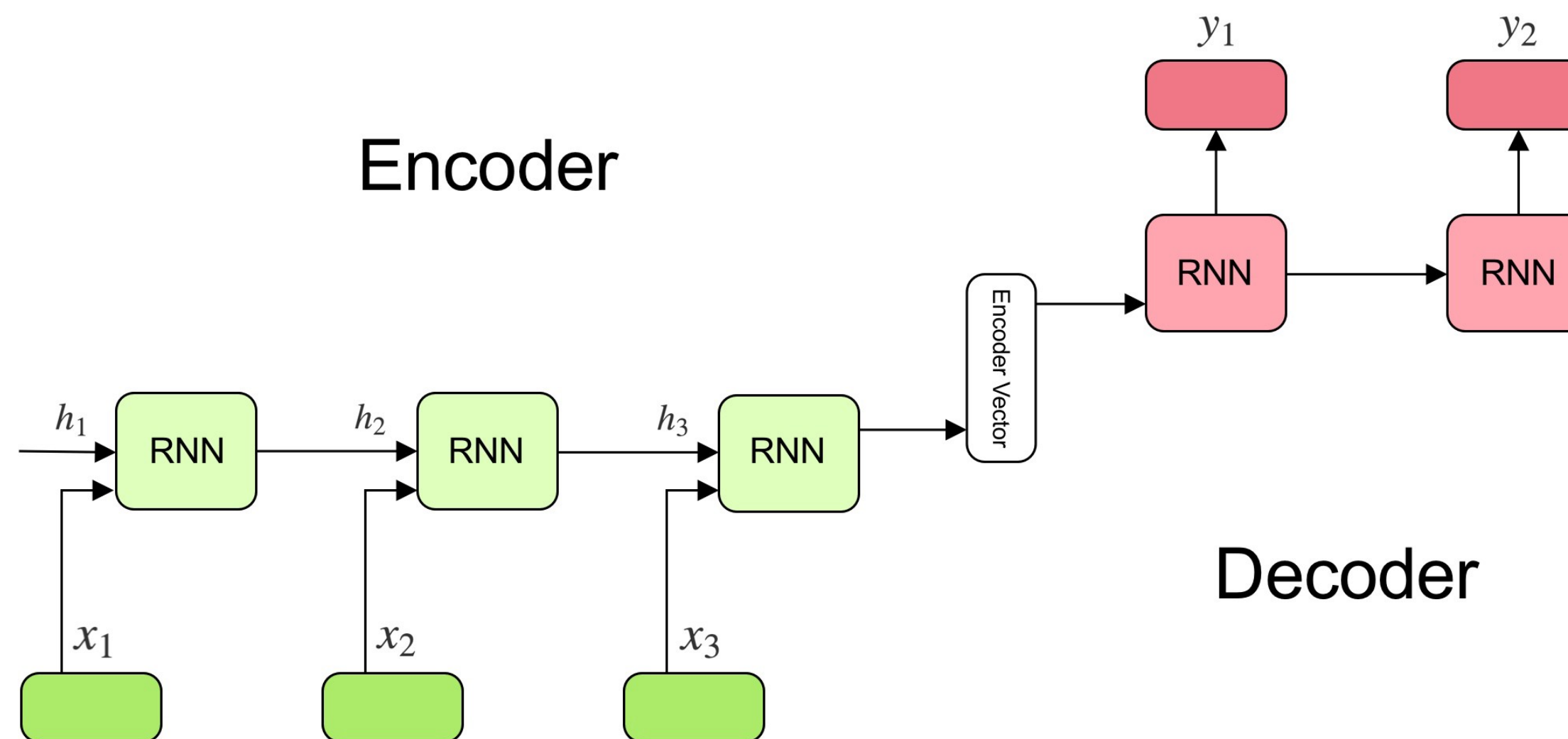
Many to Many: Question answering / Scene understanding



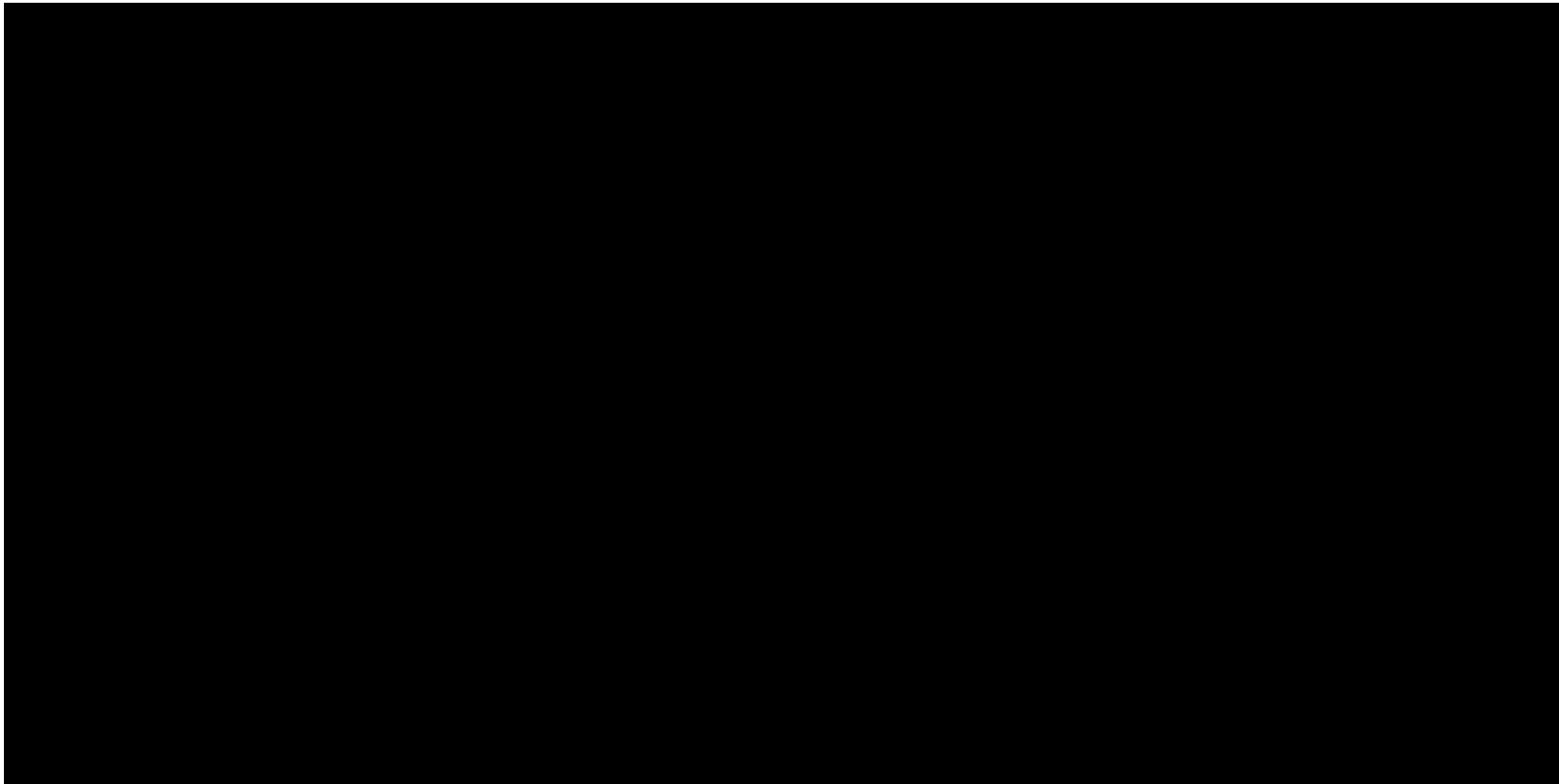
- A LSTM can learn to associate an image (static) plus a question (sequence) with the answer (sequence).
- The image is abstracted by a CNN trained for object recognition.

Many to Many: seq2seq

- The **state vector** obtained at the end of a sequence can be reused as an initial state for another LSTM.
- The goal of the **encoder** is to find a compressed representation of a sequence of inputs.
- The goal of the **decoder** is to generate a sequence from that representation.
- **Sequence-to-sequence** (seq2seq) models are recurrent autoencoders.



seq2seq for language translation



- The **encoder** learns for example to encode each word of a sentence in French.
- The **decoder** learns to associate the **final state vector** to the corresponding English sentence.
- seq2seq allows automatic text translation between many languages given enough data.
- Modern translation tools are based on seq2seq, but with attention.

References

- A great blog post by Christopher Olah to understand recurrent neural networks, especially LSTM:

<http://colah.github.io/posts/2015-08-Understanding-LSTMs>

- Shi Yan built on that post to explain it another way:

<https://medium.com/@shiyang/understanding-lstm-and-its-diagrams-37e2f46f1714#.m7fxgvjwf>